

Accepted by the Astrophysical Journal

Dust in the Small Magellanic Cloud: Interstellar Polarization and Extinction

C. V. Rodrigues¹ and A. M. Magalhães^{2,3,4,5}

Instituto Astronômico e Geofísico - USP
Caixa Postal 9638, São Paulo - SP 01065-970, Brazil
e-mail: claudia@das.inpe.br, mario@argus.iagusp.usp.br

G. V. Coyne, S. J.

Vatican Observatory
V-00120 Vatican City State, Rome, Italy
e-mail: gcoyne@as.arizona.edu

and

V. Piirola

Tuorla Observatory - University of Turku
SF-21500 Piikkiö, Finland
e-mail: piirola@sara.cc.utu.fi

ABSTRACT

The typical extinction curve for the Small Magellanic Cloud (SMC), in contrast to that for the Galaxy, has no bump at 2175 Å and has a steeper rise into the far ultraviolet. For the Galaxy the interpretation of the extinction and, therefore, the dust content of the interstellar medium has been greatly assisted by measurements of the wavelength dependence of the polarization. To the present no such measurements existed for the SMC.

Therefore, to further elucidate the dust properties in the SMC we have for the first time measured linear polarization in five colors in the optical region of the spectrum

¹Now at Inst. Nacional de Pesquisas Espaciais-INPE, Divisão de Astrofísica-DAS, Caixa Postal 515, São José dos Campos - SP 12201-970, Brazil

²Guest observer at IUE

³Visiting Astronomer, Cerro Tololo Inter-American Observatory. CTIO is operated by AURA, Inc. under contract to the National Science Foundation

⁴Visiting Astronomer, Complejo Astronomico El Leoncito, San Juan, Argentina

⁵Visiting Astronomer, European Southern Observatory, La Silla, Chile

for a sample of reddened stars. For two of these stars, for which there were no existing UV spectrophotometric measurements, but for which we measured a relatively large polarization, we have also obtained data from the International Ultraviolet Explorer (IUE) in order to study the extinction. With the help of parametrization, we attempted to correlate the SMC extinction and polarization data. In addition, we performed dust model fits to both extinction and polarization using silicate and graphite or amorphous carbon spheres and silicate cylinders. The size distribution for the cylinders is taken from a fit to the polarization and we introduce the notion of volume continuity between this and the silicate sphere size distribution.

The main results are: (1) the wavelength of maximum polarization, λ_{max} , in the SMC is typically smaller than that in the Galaxy; (2) however, AZV 456, which shows the UV extinction bump, has a λ_{max} typical of that in the Galaxy, its polarization curve is narrower, its bump is shifted to shorter wavelengths as compared to the Galaxy and its UV extinction does not conform to the Galactic analytical interpolation curve based on the ratio of total to selective extinction; (3) the 'typical', monotonic SMC extinction curve can be best fit with amorphous carbon and silicate grains; (4) the extinction towards AZV456 may only be explained by assuming a larger gas-to-dust ratio than the observed $N(\text{HI})/A(V)$ value, with a small amount of the available carbon in graphite form; (5) from an analysis of both the extinction and polarization data and our model fits it appears that the SMC has typically smaller grains than those in the Galaxy.

The absence of the extinction bump in the SMC has generally been thought to imply a lower amount or even an absence of carbon in solid form in the SMC compared to the Galaxy. Our results show that the size distribution, and not only the carbon abundance, is different in the SMC as compared to the Galaxy. In addition, and contrary to previous findings, another component besides silicates is indeed needed to provide a sizeable part of the observed extinction towards the SMC. Using the SMC as a laboratory for studying the solid component of the interstellar medium, we also discuss some of the implications of our results in view of proposed interstellar dust models.

Subject headings: ISM: dust, extinction - polarization - ultraviolet: interstellar - galaxies: Magellanic Clouds

1. Introduction

The interstellar medium (ISM) in galaxies is indicative of their evolutionary state and of their stellar populations. For instance, the Galaxy contains four times more heavy elements than the Large Magellanic Cloud (LMC) and ten times more than the Small Magellanic Cloud (SMC)

(Wheeler, Sneden & Truran 1989). The dust content of the ISM in the LMC (Koorneef 1982; Fitzpatrick 1985a) and SMC (Bouchet et al 1985; Fitzpatrick 1985b) is less than in the Galaxy and the dust is qualitatively different. In particular, the SMC has a steeper far ultraviolet (FUV) extinction curve (Prévot et al. 1984); it typically has no ultraviolet (UV) extinction bump. The SMC has also a weak infrared (IR) emission at $12\ \mu\text{m}$ and an intensity ratio $60\mu\text{m}/100\mu\text{m}$ larger than that in the Galaxy (Lequeux 1989). This would appear to indicate that star formation and evolution have proceeded at a faster rate in the Galaxy than in the LMC or SMC and/or that dust grains have formed there differently in a different environment. In fact, there is some indication that the efficiency of grain formation in the LMC and SMC may be slightly lower, albeit similar, compared to that in the Galaxy (Clayton & Martin 1985). Also, from data on M31, it is suggested that the abundance of small grains may be related to star formation rates (Xu & Helou 1994).

For these reasons and because of its proximity the SMC is an important environment in which to study dust grains. Dust may cause several observable effects: it attenuates, reddens, scatters and polarizes starlight; it absorbs and reemits radiation; it may bring about a depletion of the gas content of the ISM and may serve as a catalyst for the formation of molecules in the ISM. In the case of the SMC, the higher FUV radiation field together with the lower dust content produces an increased photodissociation of molecules that affects the properties of molecular clouds (Lequeux et al 1994). The SMC is thus an excellent laboratory to study dust in an environment quite distinct from that of the Galaxy, while at the same time allowing us to test dust models which have been proposed. We concentrate our study on the reddening and the polarization due to dust in the SMC.

It has been known for some time from IUE observations that the UV and FUV extinction relative to the visual and the IR is much larger in both the LMC (Nandy et al 1981; Koorneef & Code 1981; Fitzpatrick 1985a, 1986) and in the SMC (Prévot et al 1984) than it is in the Galaxy and the effect is larger for the SMC than it is for the LMC. The SMC is also noteworthy for the lack of the extinction bump at $2175\ \text{\AA}$ (see review by Fitzpatrick 1989). Interstellar polarization in connection with extinction in the LMC context has been studied by Clayton, Martin & Thomson (1983), Clayton & Martin (1985) and Clayton et al. (1996).

Interestingly, the SMC star AZV 456 (AZV = Azzopardi & Vigneau 1982) shows an extinction and a gas-to-dust ratio (Lequeux et al. 1984) similar to the average values in the Galaxy. The interstellar lines in this direction have typical velocities for the SMC, so that the extinction is probably not foreground (Lequeux et al. 1984; Martin, Maurice & Lequeux 1989). There is an IR extended source in the SMC located at the same coordinates as AZV 456 (LI-SMC 190: Schwering & Israel 1989), which also indicates that the extinction is within the SMC. Lequeux (1994) has raised the possibility that AZV 456 may have, in fact, a higher gas-to-dust ratio due to a possibly undetected amount of H_2 . In section 5.3.2 we show that such higher ratio is indeed required if the extinction towards this object is appropriately fit.

Classical models for fitting the wavelength dependence of the extinction by dust grains in

the ISM of galaxies generally take into account the chemical composition of the grains and their size distribution. Bromage & Nandy (1983) and Pei (1992) studied the SMC ‘typical’ extinction curve using the model of Mathis, Rumpl & Nordsiek 1977 (henceforth, MRN) with only spherical particles. They concluded that, by simply lowering the quantity of graphite grains relative to silicates in the Galactic models, it was possible to fit the *wavelength dependence* of the SMC extinction without changes in the sizes used to obtain the Galactic curve. Pei (1992) and Maccioni & Perinotto (1994) have studied the extinction in the LMC and the latter noted from their fits to the extinction that no unique solution could be obtained for the grain sizes and abundance ratios.

In the Galaxy it is known that the wavelength at which the polarization is maximum is related to the grain size (Coyne, Gehrels & Serkowski 1974). It would, therefore, be very useful to have this information for the SMC. No wavelength dependent polarization measurements have been yet published on the SMC. In this paper we present the first such observations and analyze them in light of the extinction, for which we also report a few new IUE observations. In addition, we present some model fits to these observations.

2. Data

2.1. Polarization Data

2.1.1. Observations

Polarimetric observations have been obtained during several observing runs at various observatories and with various polarimeters. The observing runs were: 1983 with the MINIPOL polarimeter (Frecker & Serkowski 1976) on the 1.5 meter telescope at the Cerro Tololo Interamerican Observatory (CTIO); 1987 with the PISCO polarimeter (Stahl et al. 1986) on the 2.2. meter telescope of the European Southern Observatory (ESO); and 1986, October 1988, November 1988 and 1989 with the VATPOL polarimeter (Magalhães, Benedetti & Roland 1984) on the 2.15 meter telescope at the Complejo Astronomico El Leoncito (CASLEO). About seventy percent of the observations were made at CASLEO.

VATPOL and MINIPOL provide on-line data reduction after each integration and/or after a series of integrations (the integration time can be freely selected). This data reduction consists of a least squares fit to a double cosine curve of the counts from two photomultiplier tubes obtained as a function of the position of a rotating half-wave plate. The mean error of the polarization is calculated from the actual deviations of the two counts from the double cosine curve; this error is typically consistent with photon-noise error, as detailed by Magalhães et al. (1984). The data from PISCO were obtained in FITS format and we wrote a special microcomputer program to calculate the polarization from the star and sky counts in a way similar to that of the other two instruments.

All data have been corrected for instrumental effects and have been standardized.

Unpolarized standard stars were measured to obtain corrections for instrumental polarization. Nightly measurements were made on highly polarized standard stars and also with a Glan prism in the beam in order to obtain the polarizing efficiencies and to standardize the polarization position angles to the equatorial system. The polarizing efficiencies were typically 98 to 99 % for VATPOL and MINIPOL. For the measurements with PISCO the efficiencies were provided to us by Hugo Schwarz of ESO. Repeated runs at CASLEO showed all corrections measured there to be stable. Corrections for bias in the linear polarization, which depend on the ratio of the error to the percentage polarization (Clarke & Stewart 1986), were also applied. We note, however, that all calculations were made using the Stokes parameters.

We combine the results from the three instrumental systems in the following way. For each star we calculate first the weighted average of the measurements made with each filter in each of the instrumental systems. We then determine the weighted mean of those averages. The results, both observed and corrected for foreground polarization (see sec. 2.1.2) are given in Table 1 where the respective columns are: (1) star number from Azzopardi & Vigneau (1982, AZV82); (2) star number from Sanduleak (1968, 1969); (3)-(5): the observed polarization, equal to the weighted mean polarization over the averages obtained from each observing run, the standard deviation of the mean and the polarization position angle in the equatorial system, respectively; (6)-(8): same as columns (3)-(5) but for the foreground corrected polarization; (9) the effective wavelength (averaged over the values for each observing run, by weighting with the mean polarization errors). The foreground-corrected polarization measurements are plotted in Fig. 1.

The targets reported in Table 1 have been selected for multifilter polarimetry from our on-going program to map the magnetic field structure of the SMC (Magalhães et al. 1990). The sample was built from the AZV82 catalog, avoiding stars with emission line spectra. This survey is presently being conducted with CCD imaging polarimetry (Magalhães et al. 1996) and the results will be reported elsewhere.

2.1.2. *Foreground Polarization Corrections*

It is necessary to correct the measured polarizations by subtracting the polarization foreground to the SMC due to dust in the Galaxy. It is expected that these corrections are important, since the interstellar reddening intrinsic to the SMC is small. We have selected published, unfiltered polarization data (Mathewson & Ford 1970; Schmidt 1976) on about 40 stars farther than 400 pc from the Sun in the direction of the stars measured in the SMC. McNamara & Feltz (1980) have shown that most of the foreground extinction to the SMC occurs within 400 pc from the Sun. Also by this selection we include most of the dust in the Galactic plane for which the scale height is 120 pc (Burton et al. 1986).

As a check on this procedure, we have also estimated the foreground polarization in two additional ways. The first of these was to average the polarization data of our survey sample

(Magalhães et al. 1990, Rodrigues 1992) for stars in the SMC which showed an observed polarization equal to or less than 0.4%. We have also averaged, again using data from our survey, polarization data for SMC stars which had an estimated color excess less than 0.09 mag. This upper limit for the foreground reddening towards the SMC is suggested by Schwering (1988); McNamara & Feltz (1980) and Bessel (1991) have suggested lower values (0.02 mag and 0.04 mag-0.06 mag, respectively). We have estimated the color excess for the SMC stars in our sample using the intrinsic colors from Fitzgerald (1970) and Brunet (1975). Both of these methods gave results that were entirely consistent with the estimates from the Galactic foreground objects (Table 2) described in the previous paragraph and which we used for correcting the SMC data.

Table 2 gives the adopted corrections for the foreground polarization towards the various regions in the SMC defined by Schmidt (1976). Our program stars are located as follows: region I, AZV 20, 126, 221; region II, AZV 211, 215, 398; region III, AZV 456. The estimated values for the foreground polarization were taken as valid for the V filter. We used the Serkowski law, with $\lambda_{max}=0.55\mu\text{m}$, to estimate the contribution in the other filters. The errors of the corrected polarization values include the increase in uncertainty arising from this correction. These are the values in Table 1. We tested the influence of changes in λ_{max} on the above estimates and on the resulting corrected data and found them to be insignificant.

2.2. UV spectroscopic data

Our UV sample consisted of three reddened stars, AZV 20, AZV 126 and AZV 211, and comparison stars necessary to obtain the extinction curves (see sec. 2.2.2). AZV 211 was our primary target because it had shown a well determined polarization curve with a small λ_{max} (Fig. 1 and Table 4). We have included in our reduction the data already published on AZV 398 (Prévot et al. 1984) and on AZV 456 (Lequeux et al. 1984) in order to test our procedure and to give homogeneity to the sample studied in the following sections. The relevant data on the reddened stars and on the comparison stars are given in Tables 3a and 3b respectively.

The UV spectral data were obtained with the International Ultraviolet Explorer (IUE, Boggess 1978a,b; Kondo 1987) in two runs: November, 1990 and September, 1991. The images were obtained with three cameras: the Small Wavelength Prime (SWP, 1200 to 2000 Å); the Large Wavelength Prime (LWP, 2000 to 3200 Å) and the Large Wavelength Redundant (LWR, 2000 to 3200 Å). We have also used some images from the IUE data archive (see last column of Tables 3a and 3b). The images are unidimensional vectors with a sampling of 1 Å.

2.2.1. Obtaining the combined spectrum of each star

Each star has been observed, sometimes more than once, in each of the two wavelength ranges. The reductions were made using the RDAF and IUEIDL packages at the University of

Wisconsin-Madison. The first procedure in the data reduction is to combine all the images of a star to one spectrum. Corrections for the time degradation of the camera sensitivity (Bohlin & Grillmair 1988a,b) are made first. At the time this reduction was done only corrections up to 1988 were available, so to correct the data obtained after that time we had to use an extrapolation. Also the cameras do not have the same efficiencies, so there may be a discontinuity in the overlap region between two spectra. It is generally assumed that the two spectra must have the same flux in the overlap region. As we are interested only in the ratio between spectra of the program and the comparison stars (see eq. 1) we have not corrected for this effect. The combined spectra did not in fact present any discontinuities.

2.2.2. Determination of the extinction curves

We have obtained the extinction curves using the pair-method (Fitzpatrick & Massa 1986) which consists in comparing two stars of the same spectral type, but with different reddening. The assumption is that the program and comparison stars have exactly the same intrinsic spectra, the observed difference being due to the foreground interstellar medium. We estimated the error in this assumption by using different comparison stars.

From the B and V magnitudes and the fluxes, ϕ_i , the normalized extinction is given by:

$$\frac{E(\lambda - V)}{E(B - V)} = \frac{2.5 \log(\frac{\phi_c}{\phi_r}) - V_r + V_c}{(B - V)_r - (B - V)_c} \quad (1)$$

where the subscripts r and c mean *reddened* and *comparison star*, respectively. Great care has been exercised in selecting appropriate comparison stars, specially for AZV 211 due to its relatively late spectral type. The comparison stars have been chosen from among SMC stars only, using the AZV82 catalog and excluding emission line stars, which are often variable and present anomalous color excesses due to circumstellar material. We also chose these unreddened stars within a spectral sub-class from AZV 211 with the purpose of matching as best we could this star's spectral type. Further, we chose to stay with comparison objects within about a magnitude of AZV 211. By using SMC stars, we also minimize the effect of metallicity differences between comparison stars and reddened stars, since two stars with the same optical spectral type but different metallicities may have different UV spectra. In addition, by using unreddened SMC objects the foreground Galactic extinction is canceled if it is homogeneous across the SMC angular field. We have later examined the UV lines to detect possible mismatches.

AZV 20 and AZV 211 have the same spectral type (A0 Ia), so we have used the same comparison stars, observed by us, for both of them (see Tables 3a and 3b). Stars of spectral type A0 Ia present some difficulties. The UV spectra change rapidly with spectral type so that a mismatch has a much greater effect than it does for stars of earlier type. Furthermore, since stars of this spectral type are cooler and their UV flux lower, it is more difficult to get a good

signal-noise ratio. AZV 126 has a spectral type (B0Iw) very similar to that of AZV 398 (B2) and AZV 456 (B0-1), so there is an overlap in the comparison stars, taken from the IUE data archive, for all three (see Table 3b). AZV 126 however is the least reddened of these three stars; the comparison stars were selected in order to provide the largest possible difference between program and comparison stars (see next paragraph). The final list of comparison stars for each program star is: for AZV 20 and 211, the comparison stars were AZV 161, 270, 504 and SK 194; for AZV 126, the comparison stars were AZV 61, 317 and 454; for AZV 398 and AZV 456, the comparison stars were AZV 235, 242, 289, 317 and 488.

As noted above, the IUE spectra have 1 \AA sampling. The extinction calculated with such a small wavelength step usually has a very poor signal-to-noise ratio. So we have also formed combined spectra with bins of 80 \AA . The flux value in each 80 \AA bin is assumed to be the sum of the fluxes in the 1 \AA bins. The extinction curves are shown in Figs. 2 and 3. The curves with 1 \AA bins (Fig. 2) are useful to identify spectral type mismatches and the noisier regions. The curves in the figures are the weighted average of the curves using different comparison stars and the error bars in the 80 \AA curves (Fig. 3) are the average standard deviation. The weights used were the values of $\Delta(B - V)$, the difference between the program star and comparison star colors given in Tables 3a and 3b. In this way we give greater weight to the reductions with the least reddened comparison stars. Also, this way of weighting is appropriate for errors dominated by measurement inaccuracies.

For AZV 211 we initially determined extinction curves from the four comparison stars listed above. We found, however, that the curve using the comparison star AZV 161 was very different than the other three curves, and we suspect that this comparison star may be reddened. We have, therefore, excluded the curve using AZV 161 from the average curve for AZV 211 and for AZV 20. The resultant average curve for AZV 211 seems to follow the SMC standard with no bump and an enhanced FUV extinction (Figs. 2c and 3c).

AZV 20 has the noisiest extinction curve (see Fig. 2a) in the sample despite the fact that it has a large color excess (see Table 3a). The systematic increase in error with increasing frequency is due to the systematic decrease in signal-to-noise (see Fig. 2a). Where the extinction curve is less noisy, the values of the extinction are close to those for the typical SMC extinction curve (compare, for example, Fig. 2a to Fig. 2c and Fig. 2d at $\lambda^{-1} \approx 5.5 \mu\text{m}^{-1}$). Its binned extinction curve shows bin-to-bin fluctuations larger than expected from the error bars.

The extinction curves which we have redetermined for AZV 398 (Figs. 2d and 3d) and AZV 456 (Figs. 2e and 3e) are in perfect agreement with those of Prévot et al. (1984) and Lequeux et al. (1984), respectively.

The extinction for AZV 126 (Fig. 2b) will be discussed in section 4.1 below. AZV 215, for which we have obtained polarization data (Tables 1 and 4), has spectra available in the IUE data bank. It has however a very small $(B - V)$ value, comparable to possible comparison stars, so we could not determine a reliable extinction curve for it.

3. Qualitative study of the optical polarization

3.1. Fits of the Serkowski-law to the SMC Polarization Data

Serkowski (1973; see also Coyne et al. 1974) has shown that the Galactic interstellar polarization can be described by the following expression,

$$P(\lambda) = P_{max} \exp \left[-K \ln^2 \left(\frac{\lambda_{max}}{\lambda} \right) \right] \quad (2)$$

where, from the observed data, the parameters P_{max} , K and λ_{max} may be obtained.

P_{max} , the maximum polarization, depends on the column density of dust as well as the magnetic field structure and alignment efficiency along the line of sight. λ_{max} is the wavelength where P_{max} occurs and it is related to size of the dust particles (Coyne et al. 1974; Chini & Krügel 1983). K describes the width of the polarization curve.

In his original work Serkowski has taken K as a constant with a value of 1.15. Codina-Landaberry & Magalhães (1976) have shown that K varied for different lines of sight. Furthermore, from model fits they showed that K could be interpreted as being related to changes in the grain size along the line of sight. Wilking et al. (1980, 1982), using an extended wavelength range that included the IR, suggested a linear relation between K and λ_{max} . Whittet et al (1992), with an even larger sample, have provided the following relation:

$$K = (1.66 \pm 0.09)\lambda_{max} + (0.01 \pm 0.05) . \quad (3)$$

We have performed fits of the Serkowski relation to our SMC data in two ways: (1) allowing K to be a free parameter; and (2) using the above relation between K and λ_{max} . Admittedly, the first approach results in larger uncertainties for the derived parameters, especially K , but we felt that a first comparison between the K values from the SMC data and those from Galactic data would be of interest. Furthermore, a comparison between the two methods might help to judge the reliability of the derived parameters.

Table 4 gives the Serkowski fit parameters. In that table, the last three columns show respectively the reduced χ^2 , the associated probabilities and the degrees of freedom. The actual fits are shown in Fig. 1. The SMC polarization data can be well fit by the Serkowski relation by using either the 2- or 3-parameter method. The only fit which is significantly improved with three free parameters is that of AZV 456.

The values of λ_{max} from the two methods agree well within the errors. P_{max} from both fits shows an even closer agreement. Larger differences are found for the K parameter, although they may still be consistent within the large uncertainties. AZV 215 has data points at only 4 wavelengths and hence the uncertainties in K are particularly large.

Table 4 shows that most of the SMC stars show λ_{max} smaller than the Galactic average, $0.55\mu\text{m}$. In particular, this is true for two of the stars with the best polarimetric signal-to-noise, AZV 211 and AZV 398, which also have a typical SMC extinction curve (sec. 2.2.2). These results are in sharp contrast, for instance, with those for the LMC (Clayton & Martin 1985). For their sample of stars with measured extinction the smallest observed λ_{max} value is $0.52\mu\text{m}$, with a median value of $0.58\mu\text{m}$. Our results will be further discussed in sec. 6.

AZV 456, which has a UV bump (sec. 4.1) and, to a certain degree, AZV 215 show λ_{max} values close to the Galactic norm. The 3-parameter fits (Table 4 and Fig. 1) indicate that their polarization curves are narrower than those for the other stars. The fact that the Serkowski fit to the ‘normal λ_{max} ’ polarization curve of AZV 456 is significantly poorer when we use the Galactic relation between K and λ_{max} may suggest that there is a different relationship between these parameters in the SMC. This suggestion is somewhat strengthened by a plot of the K vs. λ_{max} taken from the three-parameter fits in Table 4 and shown in Fig. 4. While the K - λ_{max} relation for the SMC is similar to the Galactic one, a steeper slope is suggested. More data beyond the optical domain and for more stars are needed to clarify this.

3.2. Polarization and Visible Extinction

The maximum polarization towards a given line-of-sight is related to the available amount of dust and depends on factors such as the magnetic field direction, grain alignment efficiency and the polarizing efficiency of the grains. Empirically, it is verified that for the Galaxy (Serkowski, Mathewson & Ford 1975).

$$P_{max} \leq 9.0E(B - V) . \quad (4)$$

A plot of P_{max} versus $E(B - V)$ for our sample is given in Fig. 5. We have used the 2-parameter fit P_{max} values from Table 4. We have obtained the total color excesses (Table 3a, col. 7) using the spectral type-color relation by Brunet (1975). When both our estimates and other observed values were available (AZV 398 and 456, Bouchet et al. 1985), we used the latter. For AZV 215, we used the value of $+0.12^{mag}$ (Bouchet et al. 1985). We have then corrected all color excesses by 0.05^{mag} to take into account the Galactic foreground reddening (sec. 2.1.2; Bessel 1991). The above empirical relation between P_{max} and color excess for the Galaxy is the solid line plotted in Fig. 5. It is seen that the SMC stars also obey the Galactic relation between P_{max} and $E(B - V)$.

A related quantity of interest is the average ratio $P_{max}/E(B - V)$ for the SMC objects. This is $7.2 \%mag^{-1}$ (from Tables 3a and 4). This value is comparable to the corresponding values for the Galaxy ($5.0 \%mag^{-1}$; Serkowski et al. 1975) and the LMC ($6.0 \%mag^{-1}$; Clayton & Martin 1985). Our average is biased due to our selection of the more highly polarized stars for

this multiwavelength study. Data from our survey in progress should be able in the near future to improve the estimate of this ratio for the SMC.

Serkowski et al. (1975) found a relationship between λ_{max} and $R (=A(V)/E(B - V))$, $R = 5.5 \lambda_{max}$, for stars along several lines of sight in the Galaxy. Whittet & van Breda (1978), with the aid of infrared photometry, confirmed that relation and obtained $R = (5.6 \pm 0.3) \lambda_{max}$. This correlation was re-examined and again confirmed by Clayton & Mathis (1988) using sight lines which included dense clouds as well as the more diffuse ISM. Using the data for AZV 211, 221 and 398, we obtain $\langle \lambda_{max} \rangle = (0.40 \pm 0.02) \mu\text{m}$. Bouchet et al. (1985) obtained from visual and near IR photometry for stars in the SMC a value of $R = 2.72 \pm 0.21$, from which we obtain $R/\lambda_{max} = (6.8 \pm 0.6)$, still consistent with the Galactic relation. In other words, the somewhat smaller value of R for the SMC does translate into smaller values of λ_{max} . More SMC data are clearly needed to examine this relation further.

For AZV 456, the λ_{max} values from the 2- and 3-parameter fits (Table 4, col. 2) give, using the above Galactic relation between R and λ_{max} , $3.30 \pm .24$ and $3.19 \pm .20$ for R . In other words, the star with a ‘Galactic’ extinction curve does suggest a larger value of R than that inferred from the typical SMC extinction. We have however already pointed out in sec. 3.1 that AZV 456 does not seem to conform to the Galactic K vs. λ_{max} . In addition, we shall see in sec. 4.1 that neither does its extinction curve conform in detail to that expected from a larger value of R .

4. Parametric study of UV extinction

4.1. Parametrization

In order to analyse objectively the extinction curves for the SMC we have for the first time fit them by using the parametrization of Fitzpatrick & Massa (1986). However, we have fit the parameters simultaneously, contrary to the approach of Fitzpatrick & Massa (1990). We have done this by minimizing the chi-square. The parametrization of Fitzpatrick & Massa (1990) is expressed by

$$\frac{E(x - V)}{E(B - V)} = c_1 + c_2 x + c_3 D(x; \gamma, x_o) + c_4 F(x) , \quad (5)$$

where

$$x = \lambda^{-1} ,$$

$$D(x; \gamma, x_o) = \frac{x^2}{(x^2 - x_o^2)^2 + x^2 \gamma^2}$$

and

$$F(x) = \begin{cases} 0.5392(x - 5.9)^2 + 0.05644(x - 5.9)^3, & \text{if } x \geq 5.9\mu\text{m}^{-1}; \\ 0.0, & \text{if } x < 5.9\mu\text{m}^{-1}. \end{cases}$$

We have not considered the star AZV 20 because of its very small signal-noise extinction curve (see Fig. 2a and discussion in sec. 2.2.2). We have performed the fits using the extinction curves with bins of both 1 Å (5 Å in the case of AZV 126) and of 80 Å to check the dependency of the parameters on the bin size. The results are presented in Table 5 and in Fig. 3 together with the results from the fit of the Galactic curve (Seaton 1979).

We now discuss the fits for each star with reference to Table 5 and according to the three parts of equation 5: the linear part, the Drude function fit to the bump $D(x; \gamma, x_o)$, and the exponential fit to the increasing extinction into the FUV. Column 14 of Table 5 gives the integral of the extinction curve over the bump.

AZV 211 and AZV 398 both show the typical SMC extinction (Prévot et al. 1984) with no bump and a rapid increase in the UV and FUV extinction (Table 5, col. 8). Although these stars do not present the bump, any oscillation in the extinction curve might be interpreted artificially by the code as a small bump (see Table 5, cols. 10-13 and Fig. 3). For that reason, we have also performed the fits without the Drude function component. There was however no significant difference in the resultant parameters.

The extinction curve of AZV 456 is very similar to that for the Galaxy (Fig. 3; Lequeux et al. 1984; see entries for AZV 456 and the Galaxy in Table 5) and, in fact, its extinction curve has been often referred to as a 'Galactic-type' curve. However, our fits show that its bump is shifted to the blue ($x_o = [4.66 \pm 0.02]\mu\text{m}^{-1}$, Table 5) with respect to the Galactic average ($x_o = [4.596 \pm 0.019]\mu\text{m}^{-1}$). For comparison, the largest value of x_o in the sample of Fitzpatrick & Massa (1986) is $4.63\mu\text{m}^{-1}$. The width and intensity of the bump for AZV 456 are within the range of those for the Galaxy. In contrast, the three sight lines which show $x_o > 4.65\mu\text{m}^{-1}$, seen through dense material, all appear to be associated with broad bumps (Cardelli & Savage 1988; Cardelli & Clayton 1991; Mathis 1994).

From studies of several Galactic sight lines, which included diffuse, dark cloud and star formation regions, Cardelli, Clayton & Mathis (1989) have shown that there is an average extinction law over the wavelength range $3.5\mu\text{m}$ to $0.125\mu\text{m}$ which is applicable to such environments. This mean extinction law, $A(\lambda)/A(V)$, depends only on the parameter R . They have noted, however, that a few sight lines, which included ones with broad bumps and those towards the LMC, did not conform to such a law. In Fig. 6 we plot the UV extinction curve of AZV 456 with the analytical law of Cardelli et al. (1989) for the values of $R = 2.72, 3.1$. It can be seen that the observed and analytical curves are discrepant, specially around the bump region, meaning that the line of sight to AZV 456 does not conform to the single parameter interpolation that performs well for the Galactic environs.

Among stars in our Galaxy which also present non-standard UV bumps, HD 62542 has the most extreme bump, centered at $4.74\mu\text{m}^{-1}$ (Cardelli & Savage 1988). Interestingly enough, the FUV extinction curve of HD 62542 and the SMC are actually very similar. However, its bump is extremely shallow and its intensity is quite different (lower) compared to the Galactic average and AZV 456. In addition, our multicolor polarimetry of HD 62542 (reported by Clayton et al. 1992) shows that its λ_{max} value is $0.59\mu\text{m}$, quite different from the low λ_{max} values for the SMC (Table 4). This stresses the value of linear polarimetry in providing additional, independent information about the grains. In fact, in sec. 5 it will become clear that detailed simultaneous fitting of both extinction and polarization is more restrictive on the grain model parameters.

The parametrization of the extinction curve for AZV 126 with 1 \AA bins did not converge. This may have been due to the available signal-to-noise or some spurious effect in the extinction curve that the parametrization fit tried to include. We have hence fit eq. 5 to an extinction curve binned to 5 \AA for AZV 126. This allowed a more reasonable parametrization. It nevertheless shows an abnormally small slope for the linear part (Table 5, col. 4). The Drude function fits (Table 5, cols. 10-13) indicate that it may have the extinction bump but shifted to the blue (Table 5, col. 12) with regards to both the Galaxy and AZV 456. The bump is also abnormally wide (Table 5, col. 10), although its intensity is within the Galactic range. The rise into the UV and FUV (Table 5, col. 8) is intermediate between that typical for the SMC and that for the Galaxy. The extinction curve for AZV 126 has a large intrinsic uncertainty and it must be viewed with caution.

4.2. Correlations between extinction components

Although the small number of extinction curves available for the SMC makes any search for correlations between the parameters difficult, there are tentative indications of correlations between the linear coefficients (c_1 , c_2) and the coefficient (c_4) of the linear and FUV portions, respectively, of the extinction curves (eq. 5). These are shown in Fig. 7. The point with large error bars in that figure corresponds to parameters for the Galactic curve given in Table 5. The large errors are due to the fact that relatively few data points were conveniently tabulated for the fit to the Galactic curve. Those error bars are hence very conservative.

Figure 7 shows that the FUV curvature for the SMC, c_4 , is anti-correlated with the constant component, c_1 , and positively correlated with the slope of the linear component, c_2 . In fact, the parameters c_1 and c_2 are perfectly correlated (Fitzpatrick & Massa 1988; Jenniskens & Greenberg 1993) and c_1 is not an independent parameter. If the FUV curvature does increase at the same time as the contribution of the linear component to the extinction, this can be interpreted as the result of a simultaneous decrease in the average size of the grains responsible for these various parts of the extinction curve. For the Galaxy no correlation is found between the linear rise and the extinction in the FUV (Jenniskens & Greenberg 1993). This may be a further indication of the differences between the ISM in the SMC and the Galaxy, where the correlation found may simply

signify the increasingly larger number of smaller particles as we go from the Galaxy to the SMC.

The fact that AZV 211 and AZV 398 show a sizeable contribution to the FUV term in their extinction curves, quite larger than that of AZV 456, is consistent with what is found for the Galaxy, for which no positive correlation exists between the bump and the FUV curvature (Greenberg & Chlewicki 1983; Jenniskens & Greenberg 1993). In the Galaxy, the linear rise part (c_1 , c_2) of the extinction curve is systematically less in dense media (Cardelli et al. 1989; Jenniskens & Greenberg 1993). The behavior of the extinction curve for AZV 456 seems to follow the same trend. In contrast, the Galactic object HD204827 shows a steep FUV rise (Fitzpatrick & Massa 1990) while at the same time showing small λ_{max} (Whittet et al. 1992; Clayton et al. 1995), in line with the typical SMC sight lines. In section 6, we will return to this discussion.

5. The SMC Data and Dust Models

We have tried to fit the SMC data using the MRN grain model (Mathis, Rumpl & Nordsieck 1977). In this model the grains are homogeneous spherical particles of silicate and of graphite with a -3.5 power law size distribution. The sizes range from $0.02\mu\text{m}$ to $0.25\mu\text{m}$ for silicate grains and from $0.005\mu\text{m}$ to $0.25\mu\text{m}$ for graphite grains. There are two approaches to the polarization within the context of the MRN model. Mathis (1979, 1986) introduced an additional population of elongated silicate grains (cylinders). A single size distribution describes both the spherical and the elongated silicates. From a minimum grain radius, a_-^{sil} , until an intermediate radius, a_p^{sil} , the grains were assumed to be spherical (or not aligned), and from then up to a maximum radius, a_+^{sil} , they were taken as aligned cylinders. This case will be called the M79 model. Mathis (1986, hereafter M86) proposed a modification to the above scenario. The polarizing material would consist of silicate particles containing inclusions of ferromagnetic material in order to make the alignment more efficient (Jones & Spitzer 1967). The number of these inclusions increases with grain size in such wise that larger grains have a greater probability of being aligned. Although the size distribution is the same as in M79 model, in this case there is a probability function which must be multiplied by the size distribution of cylinders in order to give the number of aligned cylindrical grains contributing to the polarization. To calculate the extinction in the M86 model, we have assumed that all cylindrical grains are aligned.

We introduce two innovations to the above models. First, we attempt to fit the observations by using the polarization and the extinction together. The implications on the extinction curve of including silicate cylinders has not been studied in detail by Mathis (1979, 1986). Kim & Martin (1994, 1995) have derived the dust particle mass distribution from the polarization curve for the Galaxy, although, as noted by them, extinction and polarization curves still need to be consistently and simultaneously interpreted. Thus, to the best of our knowledge such combined fits have not been attempted previously. To carry out these fits, it is necessary for us to adopt a model for the degree of alignment as a function of grain size, and an axial ratio for the aligned grains. At the end of the fitting process we look at the predicted ratio $P(V)/A(V)$ to check the

validity of these assumptions. It is important to realize (sec. 5.2) that the combination of shapes may affect the extinction in addition to the polarization. Secondly, we introduce *volume* continuity as an alternative to *size* continuity. The size distribution, $n(a)$, can be algebraically represented as

$$n(a) = N f(a),$$

where a is the particle radius and $f(a)$ describes the shape of the size distribution. N , called hereafter number constant, is related to the absolute number of grains. This constant is dependent on the elemental abundance (gas phase plus dust) and on the depletion of the main grain constituents. We use the word depletion to mean the fraction of a given chemical element locked up in the grains. The abundances of interest are those of carbon (C) and silicon (Si).

In the single size distribution of Mathis (1979), when silicate cylinders and spheres have the same number constant, the Si fraction in each population is automatically fixed by one boundary condition: the number of cylinders and spheres at the radius a_p^{sil} must be the same. Hereafter, we call this case *size continuity*. We have in addition studied the influence of a different boundary condition on the distribution of spheres and cylinders. We employ the same shape, $f(a)$, for the size distributions of both populations, but their number constants are different. Specifically, we have calculated them in such a way that the volume distribution is continuous, i.e., the boundary condition is such that the total volume occupied by the spherical and by the cylindrical grains of size a_p^{sil} must be equal. This will be called *volume continuity*. For example, for the elongation of two adopted here for the cylindrical particles, the number of spheres is larger by a factor three. This results in a larger relative contribution by spherical particles in the case of the volume continuity as compared to size continuity.

The optical properties for the so-called astronomical silicate have been taken from Draine & Lee (1984), who made a synthesis of laboratory and astronomical data. Its properties are quite similar to olivine ($[Mg, Fe]_2SiO_4$) and it shows the characteristic change in the UV slope of the extinction curve around $6.5\mu m^{-1}$. For enstatite ($[Mg, Fe]SiO_3$), we have used the optical constants obtained by Huffman & Stapp (1971). These constants are given only for the optical and UV. This material was employed by Bromage & Nandy (1983) in their fit to the typical extinction curve for the SMC. The index of refraction for graphite has been taken from Draine & Lee (1984). We use the "1/3-2/3" approximation to calculate the extinction coefficients. Draine & Malhotra (1993) have recently shown that this procedure is sufficiently accurate. For the amorphous carbon we have adopted the constants of Duley (1984).

5.1. Fit procedure

Our approach was to first fit the polarization, the wavelength dependence of which determines the size distribution parameters of the cylindrical silicate population. Then from the maximum polarization of the fit we determine the Si abundance in the form of cylindrical grains. Next we fit the size distribution parameters of graphite and spherical silicate grains in order to reproduce the

extinction curve, assuming the cylindrical population fixed.

The minimum and maximum sizes of the cylinder silicate distribution were obtained from a chi-square (χ^2) minimization procedure applied to the polarization curve normalized to the maximum polarization. We assumed perfect spinning alignment (Chlewicki & Greenberg 1990 and references therein) and three values of the angle between the direction of the magnetic field and the plane of sky, γ : 10, 30 and 60 degrees. Next we calculated the necessary Si abundance (i.e., Si/H) to reproduce the polarization in the V filter. For that we must know the color excess, $E(B - V)$, and the gas to dust ratio, $N(H)/E(B - V)$ (e.g., Casey 1991), since we are in effect fitting $P(V)/N(H)$. Assuming a given continuity (size or volume), we can calculate the number constant of the spherical silicate distribution, whose maximum size is fixed by the cylinder sizes. Therefore, for a given C depletion, we have only to fit the minimum size of spherical silicates and the size parameters of the C grain population (again the slope of the size distribution was held fixed, for simplicity). We also apply a chi-square minimization procedure to the $A(\lambda)/N(H)$ data. All the extinction curves were fit using both size and volume distribution continuities and various carbon depletions.

5.2. Fits to Galactic Data

In order to compare the SMC environment with that of the Galaxy we first discuss fits to the polarization and extinction in the latter. In Fig. 8 and Table 6 we present fits to the polarization curve which was considered as a Serkowski law with $\lambda_{max} = 0.55\mu\text{m}$ from optical studies. Presently, the interstellar polarization curve is known throughout a much wider wavelength range, which could provide stronger constraints on the size distribution (e.g., Kim & Martin 1994; Anderson et al. 1996). However we decided to consider only the optical range, which is the one we have available for the SMC (sec. 2.1). To obtain the value of $P(V)/N(H)$ to fit, we adopted $P_{max}/E(B - V) = 9$ (the maximum observed, and $P(V) \approx P_{max}$), $N(H)/E(B - V) = 5.848 \cdot 10^{21} \text{ cm}^{-2}$ (Bohlin, Savage & Drake 1978), and $R = 3.1$. The fractional error in $P(\lambda)$ was taken to be 10%. In Figure 9 the scale of P is in fact arbitrary, corresponding to $N(H) = 6.433 \cdot 10^{20} \text{ cm}^{-2}$, or $E(B - V) = 0.11$. We have assumed the following abundances: Si/H = $3.55 \cdot 10^{-5}$ (7.55 dex) and C/H = $3.63 \cdot 10^{-4}$ (8.56 dex) (Anders & Grevesse 1989). In Fig. 8 we show fits for $\gamma = 30^\circ$, although the wavelength dependence of the Galactic polarization curve is well fit for all γ values used. We found local chi-square minima for the various size distributions listed in Fig. 8. Below we will study the behavior of the extinction curve for these different cylinder size distributions. The different size parameters obtained for a given γ differ in range, but have practically the same $\langle a \rangle$ (Table 6). For $\gamma = 60^\circ$ the required Si abundance is greater than that available in the Galactic ISM. In this case we have assumed a $P_{max}/E(B - V)$ of 2.0 and 5.0 (Table 7, col. 16). This lowers the amount of Si needed to fit the polarization.

We now proceed with fits to the Galactic extinction curve. These are shown in Fig. 9 and Table 7. We see from Table 7 that the best fit to the Galactic extinction curve for each cylinder

parameter set is systematically found for a Carbon depletion of about 0.70 and volume continuity (Fig. 9). The curves depart from the observed Galactic curve in the optical range and this is due to the adopted size distribution, as demonstrated by Kim, Martin & Hendry (1994). The better agreement of the extinction curve using volume continuity would seem to favor a situation in which the smaller grains are more numerous than predicted by the power law of index -3.5. This may be accomplished by a steeper power law or a discontinuous size distribution from spheres to cylinders, as we assumed.

In any case, an important point is that, if we start with the size distribution of spherical silicates that, together with graphite, fit the extinction curve, a simple replacement of the larger silicate particles by cylinders that fit $P(\lambda)$ will *not* fit the extinction any longer.

A glance through the fits for the Galaxy in Table 7 reveals that there is a tendency of both the M79 and M86 models with perfect spinning alignment to provide relatively high $P(V)/A(V)$ values. This would indicate that perfect spinning alignment is not a necessity (see also Kim & Martin 1995).

5.3. SMC fits

We have performed polarization and extinction fits for two stars in the SMC: AZV 398 and AZV 456, since they have relatively high values of polarization and better determined extinction curves. Furthermore, they may represent lines of sight with different grain characteristics. Although their UV extinction curves are different, their IR extinction seems to be very similar according to Bouchet et al. (1985). We have hence used the value of R ($= 2.72$) from the latter reference. The abundances of carbon ($C/H = 6.455 \cdot 10^{-5}$, or 7.80 dex) and silicon ($Si/H = 7.59 \cdot 10^{-6}$, or 6.88 dex) have been taken from Dufton, Fitzsimmons & Howarth (1990), which provides the abundances of C, Si and other elements in the atmosphere of a main sequence B-type star in the SMC. We assume that these represent the present ISM abundance in that galaxy (Pagel 1993). For our subsequent analysis, we assumed the following $N(HI)/A(V)$ values: for AZV 398, $4.1 \cdot 10^{22} \text{ cm}^{-2}$; for AZV 456, $6.9 \cdot 10^{21} \text{ cm}^{-2}$ (Bouchet et al. 1985).

5.3.1. AZV 398

In Fig. 10 and Table 6 we present the model fits to the polarization of AZV 398 which shows the highest polarization in our SMC sample (sec. 2.1). The polarization decreases rapidly from the R to the I filter and not all of the models fit those points equally well. We also performed the fits by replacing astronomical silicate with enstatite. The value of $\langle a \rangle$ obtained with enstatite is slightly larger than that obtained using astronomical silicate as a consequence of the differences in optical constants of those materials.

In Fig. 11 and Table 7 we present the model fits to the extinction of AZV 398. We obtain a good fit by using enstatite plus graphite and volume continuity (Table 7 and Fig. 11a). In this case, the extinction curves of each population can be combined to give a practically linear curve. 40% of the available C in the SMC is used. This fit, however, requires approximately 30% more Si than the available in the SMC ISM (Table 7, col. 14). Also of note is the relatively high value of the lower limit of the graphite size distribution ($0.0372 \mu\text{m}$, Table 7) of this fit, which prevents the extinction curve to show an UV bump.

We have examined the consequences of replacing the population of graphite grains by one of amorphous carbon particles. As seen in Fig. 11b we can reproduce the AZV 398 extinction curve in shape and level. The amorphous carbon extinction fits specially well the FUV and because of that the fits with large C depletion tend to have smaller χ^2 . Also, we have obtained a larger number of good fits with amorphous carbon compared with fits using graphite. The required amount of Si and C in grains is about 70% and 80%, respectively, of that available in the SMC (Table 7).

The required mass in solid carbon obtained from the AZV 398 fits (in boldface in Table 7; Fig. 11) varies from 10% (with graphite) to 20% (with amorphous carbon) of the corresponding value derived from the fits to the Galaxy. They reflect the product (C-abundance)*(required depletion) from the Galaxy to the SMC. As the required depletions are similar from one galaxy to another, that value follows basically the C-abundance ratio between the two galaxies. The same occurs with the total grain mass (carbonaceous + silicate grains). However, in the SMC the fraction of mass in cylindrical grains relative to the total silicate grain mass (38% with graphite and 22% with amorphous carbon) is significantly smaller compared to the corresponding value in the Galaxy (about 70%). Also, the upper limit of the carbon particle size distribution (Table 7, col. 10) is significantly smaller than that in the Galaxy for most of the (and certainly for the best) SMC fits. The amorphous carbon size distribution is also narrower than that for the Galaxy. In other words, the dust particles are on average smaller in the SMC as compared to the Galaxy. At the same time, note the absence of the very small graphite particles that produce an extinction bump.

Another important corollary of these AZV398 fits is that the typical SMC extinction curve cannot be adequately fitted by using silicates alone, as previously advocated (Bromage & Nandy 1983; Pei 1992), unless the Si abundance in the SMC ISM is significantly revised upwards, an unlikely event. Therefore, we feel that use of the dust properties of models that employ silicates only should be exercised with caution.

5.3.2. AZV456

In Fig. 12 and in Table 6 we present some of the best fits obtained for AZV456 which has an unusually narrow polarization curve. These occur for either small values of γ or for relatively

narrow size distributions. The M79 fit with $\gamma=10^\circ$ and astronomical silicates (solid line) presents a significant improvement relative to the $\gamma=60^\circ$ fit with enstatite (dotted line). At the same time, the low γ fits require less Si and provide less extinction (see below). Values of γ smaller than 10° were also tried but did not improve the fits. Some curves from models with narrow size distributions present an oscillating spectral dependence, especially for larger values of γ . The polarization curve of a single grain is characterized by ripples which are usually averaged out by a size distribution, except when the distribution is very narrow.

These fits are characterized by average sizes similar to those for the Galaxy, confirming the usual relationship between λ_{max} and the average sizes. Wilking et al. (1980) suggested that an increase in the real part of the index of refraction can produce progressively narrower polarization curves. We have made some fits using hypothetical compounds, with a wavelength-independent index of refraction, in order to gain some insight into this. We have varied the real part of the index of refraction from 1.7 to 2.0 and the imaginary part from 0.01 to 0.05 but such changes in the index of refraction do not seem to be large enough to improve the results. Spheroids provide narrower polarization curves than do infinite cylinders (Wolff et al. 1994; Kim & Martin 1995). Whether these particle types can improve the fits remains to be verified.

Fitting the extinction of AZV 456 presents an interesting challenge, given a Galactic gas-to-dust ratio and the low SMC metallicity. We first try, as usual, to fit AZV 456 with silicate cylinders and spheres and with carbon spheres but, because of the observed UV bump, we must now add graphite spheres. The cylinders already use a sizeable fraction of the available Si (Table 6, col. 6). Providing the observed extinction levels by adding spherical particles will require the addition of Si several times that available in the SMC. Graphite particles reproduce the bump and provide some optical extinction, with a relatively small UV contribution. It is clear that there will not be enough material available in the SMC ISM capable of providing the needed extinction towards AZV 456.

A possible solution out of this conundrum is to resort to the possibility that AZV 456 may actually have a larger gas-to-dust ratio, closer to the more typical SMC values. Lequeux (1994) has argued for possible H_2 towards the AZV 456 line-of-sight and we noted in the Introduction that there is an IRAS extended source towards this same direction. Let us assume that the gas-to-dust ratio towards AZV 456 equals the $N(HI)/A(V)$ ratio shown by AZV 398 (i.e., a factor of about 6 higher than the observed $N(HI)/A(V)$ ratio for AZV 456). For the cylindrical grains, we take one of the grain populations that fits the polarization (Fig. 12), with a correspondingly lower Si/H abundance. The resultant extinction fit is shown in Fig. 13. Note that the 'bluer' bump of AZV 456 is now evident in Fig. 13. The cylinders use a relatively large amount (80%) of the available Si and provide a sizeable contribution to the extinction. The total Si used is about 50% more than the amount available. Our purpose here is not to opt for a particular fit, given the uncertain gas-to-dust ratio towards AZV 456, but only to show that it may be possible to fit the extinction towards this star if we assume a higher gas-to-dust ratio in its line-of-sight.

As a matter of fact, given that amorphous carbon (and silicates) explains so well the typical SMC extinction (sec. 5.3.1), it is quite reasonable to expect this component to be present towards AZV 456 as well. The inclusion of amorphous carbon in a model will lower the amount of Si needed, as this unpolarizing, carbon component will provide some of the needed extinction as well as lower the $P(V)/A(V)$ ratio. Additionally, the best fits to the polarization of AZV 456 actually do use a small amount of Si (Table 6). The inclusion of amorphous carbon implies, of course, a larger number of free parameters. We have however used the same size distribution for amorphous carbon obtained from the AZV 398 extinction fits and verified that the overall extinction towards AZV 456 may indeed be obtained.

6. Discussion

6.1. The SMC Interstellar Polarization and Extinction Data - What do they mean?

We now wish to discuss the data presented on the sample of stars in the SMC for which we have available both extinction curves and/or wavelength dependent polarization data.

Our extinction data suggest a correlation between the FUV curvature and the linear portion of the extinction curve (sec. 4.2). The stars for which the FUV contribution is more important, AZV 211 and AZV 398, do not show the bump, so the FUV curvature cannot be attributed to the same grains producing the bump. Further, these two stars show λ_{max} smaller than the Galactic average. Other SMC stars also present small λ_{max} values (Table 4, col. 2). Of the two stars in the SMC which have larger λ_{max} values, similar to those for the Galaxy, the one with the best signal-to-noise, AZV 456, has a well determined extinction curve (Prévot et al. 1984; sec. 4.1). This star does show the bump and its λ_{max} value indicates that it is also characterized by grains larger than those found for the other sight lines in the SMC. It is also of interest to note that from observations in our Galaxy the bump is usually not polarized (Clayton et al. 1992; Anderson et al. 1996), so that the grains producing the bump are either spherical or not aligned.

It is tempting to conclude that the bump in the SMC would be present only along lines of sight characterized by large λ_{max} . This conclusion might be tenuous, since stars with both polarization and extinction curves reliably determined are very few in the SMC and there is only one known line of sight which shows the bump. However, it is rather remarkable that AZV 456 has an extinction curve similar to that for the Galaxy (Prévot et al. 1984; sec. 4.1) and a λ_{max} value similar to the Galactic average (sec. 3.1). All of the remaining stars in the sample of about 20 stars of Bouchet et al. (1985) and Fitzpatrick (1985b) show a gas-to-dust ratio ($N(HI)/A(V)$) roughly 10 times the Galactic average. The 3 stars in the sample of Prévot et al. (1984), which have this high gas-to-dust ratio, do not show the bump. In addition, in our sample of stars those which do not show the bump show small λ_{max} values. Extending the arguments of Fitzpatrick (1989) to include polarization data, we may say that, if the high gas-to-dust ratios are produced by conditions which also give rise to the typical SMC extinction law and small λ_{max} values, then

our polarization measurements, as well as the extinction law of Prévot et al. (1984), may indeed represent the typical extinction and polarization properties of the dust in the SMC.

The λ_{max} results from our polarization data are important in order to improve the constraints on dust models for the SMC and as a test for inferences based solely on extinction data. Bouchet et al. (1985) point out that the value of R they have determined for the SMC, slightly smaller than the Galactic value, might suggest that the graphite grains would play a smaller role in the visible/IR. According to them, the size distribution of silicate grains, in the context of the MRN model would then have to be shifted towards larger grains. Our fits to the observations show that the opposite is actually true, λ_{max} is in general smaller than in the Galaxy. While it might be expected that λ_{max} would depend on how the alignment mechanism works as a function of size, studies of the correlation between extinction and polarization (Serkowski et al. 1975; Whittet & van Breda 1978; Clayton & Mathis 1988; sec. 3.2) for the Galaxy for several types of sight lines suggest that the populations producing extinction and polarization would seem to be affected similarly by the environment and that λ_{max} variations originate mainly from differences in the size distributions rather than variations in the alignment of particles (Clayton & Mathis 1988).

The λ_{max} results can be interpreted in terms of the dust grain sizes. Values of λ_{max} close to $0.55\mu\text{m}$ indicate that the grains towards AZV 456 have average sizes close to those in the Galactic diffuse ISM, although with a narrower size distribution. Inspection of the line of sight to AZV 456 using the catalog of SMC IRAS sources of Schwering & Israel (1989) shows that there is an extended IR source towards that object. This line of sight might then indeed not represent the typical line of sight through the diffuse ISM in the SMC, as discussed earlier in this section.

The lines of sight with smaller λ_{max} would evidence smaller average grain sizes. They are associated with no bump in their UV extinction curves, that is, with the extinction law which is considered typical of the SMC (Prévot et al. 1984). The correlation between the FUV curvature and linear part of the extinction curve, suggested by the data (sec. 4.2), indicate smaller average grain sizes producing the typical SMC extinction. The smaller average grain sizes inferred from our polarization data and model fits strengthen this interpretation.

6.2. The SMC environment and dust models

As outlined in the Introduction, the SMC is a valuable laboratory for studying several aspects of the evolution of the dust content of the ISM in galaxies (Westerlund 1989, 1990). The UV bump in the Galactic extinction curve is thought to be produced by carbon (graphite) grains. Consequently, the lack of the bump in the SMC extinction curve is usually associated with a small quantity of carbon grains. However, there is no evidence for a carbon deficiency in the ISM of the SMC. Despite the comparison between stellar dust injection and depletion by star formation and shocks in the interstellar medium, many of the grains containing carbon are thought to come from carbon stars (e.g., Gehrz 1989). The relative number of carbon stars to normal stars in the

post main-sequence stages of stellar evolution is actually greater in the SMC than in the Milky Way (Lequeux 1988 and references therein). Also, the C/Si ratio seems to be comparable to the Galactic one (Dufton et al. 1990, see Sec. 3). On the other hand, it has been argued that amorphous carbon grains are a more plausible interstellar component than graphite (Bussoletti, Colangeli & Orofino 1988 and references therein). Studies of interplanetary dust show that graphite is present only in trace amounts (Nuth 1985). Amorphous carbon has also been detected around R CrB stars (Hecht et al. 1984).

The typical SMC extinction curve, shown by AZV398, can be best fit with amorphous carbon grains rather than with graphite grains (sec. 5.3.1). Moreover, with graphite the required Si abundance is somewhat greater than that available in the SMC. Support for an amorphous carbon component to the AZV 398 extinction is additionally provided by the star HD 89353 (=HR 4049) whose extinction curve has no bump but a high, quasi-linear rise into the UV produced by grains in a circumstellar envelope (Buss, Lamers & Snow 1989). Among the stars in the Galaxy it is one of the poorest in metals and richest in hydrogen and carbon. Blanco, Fonti & Orofino (1995) were able to fit its extinction using optical constants of amorphous carbon rich in H. On the other hand, Mennella et al. (1995) show that initially H rich amorphous carbon grains progressively lose their H as annealing occurs. The extinction bump varies in position and strength according to the annealing temperature. How could H-rich amorphous carbon survive in the SMC ISM, an environment with a high UV ISRF? What is the role of the ISM metallicity in grain evolution? Jenniskens et al. (1993) suggested that an icy mantle formed in molecular clouds can be transformed to an organic residue due to action of the FUV radiation, and that a prolonged exposure to this radiation can lead to the formation of amorphous aromatic carbon.

In the line of sight to AZV456, which seems to have larger grains, there is an IR emission associated with cold dust. This can be considered, therefore, as a region with density enhancement, similar to the Galactic molecular clouds. The small gas-to-dust ratio towards this region could also be an indication of the presence of molecular hydrogen (Lequeux 1994). If this indeed happens, we can expect that the enhanced density will lead to the accretion of smaller grains on to the larger ones. This will increase the average size and reduce the width of the grain size distribution, as seen in the AZV456 results. If we believe that (part of) the line of sight to AZV 456 is really characterized by higher densities, then the grains could be shielded from the strong ISRF, and the carriers of the 2175Å bump could survive. Recently, Andersson & Wannier (1995) found a Galactic molecular cloud whose dust is characterized by normal values of λ_{max} and large K.

It has been suggested (Sorrel 1990) that carbon is transformed into graphite in the ISM by an annealing process caused by the interstellar radiation field (ISRF). The SMC would, in that case, be a privileged site for graphite formation because the ISRF is greater there than in the Galaxy (Lequeux 1989). But that does not seem to be the case, since the UV bump is not generally observed.

Actually, the higher ISRF in the SMC might have a bearing on the absence of a UV bump

in the SMC typical extinction curve. Leene & Cox (1987) found a correlation between the $60\mu\text{m}/100\mu\text{m}$ brightness ratio, a measure of dust temperature, and the height of the Galactic UV bump in the sense that the bump gets weaker when the $60\mu\text{m}/100\mu\text{m}$ ratio (and presumably the ISRF) gets higher. They suggested that the particles responsible for the UV bump are very sensitive to the ISRF intensity. Jenniskens & Greenberg (1993) also found that the bump is sensitive to strong UV radiation fields from their studies of Galactic extinction curves and the environment.

We now wish to point out some implications of the SMC data and the hypothesis of Polycyclic Aromatic Hydrocarbons (PAHs). Jenniskens, Ehrefreund & Désert (1992) have found a correlation between the amount of FUV rise (c_4 , sec. 4.1) and the CH abundance in the line of sight to several Galactic stars. Since CH is directly proportional to molecular hydrogen, they suggested that the carrier of the FUV rise coexists with the medium containing H_2 . They also suggested that the FUV rise is associated with the PAHs. As we have seen, AZV 456 is related to an IR extended source and its smaller gas-to-dust ratio suggests the presence of H_2 . However, it is precisely AZV 456 which shows a small value of c_4 (Table 5 and Fig. 7).

A related question concerns the PAH hypothesis and the IR emission of the SMC. Sauvage, Thuan & Vigroux (1990) presented the colors of the IRAS IR emission of the LMC and SMC and correlated them with the age and metallicity of the underlying stellar populations. Lequeux (1989) has nicely reviewed these and other IR data and their implications for the interstellar dust in the Magellanic Clouds. The integrated $12\mu\text{m}$ emission of the SMC (Rice et al. 1988, Schwering 1988) is specially low among irregular galaxies, suggesting that the PAHs, believed to be responsible for such emission, are less abundant, perhaps having been destroyed by photodissociation by the more abundant FUV photons. This could be due to the larger ISRF in the SMC. The IRAS color-color diagrams suggest that the SMC may be rich in small ($\lesssim 0.05\mu\text{m}$) grains responsible for the extinction shortwards of 2000\AA . While the SMC extinction and the polarization data we provide herein support the abundance of small grains, the steep FUV extinction and low $12\mu\text{m}$ emission seem to rule out the PAHs as suggested by Désert, Boulanger & Puget (1990).

7. Summary

In order to study the grains in the SMC, which has an extinction curve very different from that for the Galaxy, we have obtained the first wavelength dependent polarization measurements for stars in the SMC. From an analysis of these and the extinction curves, for which we present some new IUE data, for a small sample of stars we reach the following conclusions:

- the wavelength of maximum polarization, λ_{max} , determined from a fit of the Serkowski curve to the new polarization data, is generally smaller than in the Galaxy;
- for AZV 456, the single well-studied case which shows the extinction bump at 2175\AA ,

λ_{max} is typical of that in the Galaxy; at the same time the bump for this star is shifted to the blue, as compared to the Galaxy, and its polarization curve is narrower;

- the FUV curvature and the linear component of the extinction curve increase simultaneously for stars with small λ_{max} .

We attempt to fit both the extinction and polarization data for stars in the SMC by varying the mean size and the size distribution of the grains within the framework of the MRN model and introducing the notion of volume continuity. Our results are:

- The AZV 398 (i.e., the typical SMC) extinction curve is best fit using, in addition to silicates, amorphous carbon instead of graphite. The polarization data and the polarization and extinction fits indicate smaller grains in the SMC as compared to the Galaxy. Contrary to earlier belief, silicate alone cannot provide the amount of extinction observed towards the SMC, despite its providing an approximately correct wavelength dependence;
- It appears that for AZV456 there may be a contribution, not yet accounted for, of H_2 to the actual ratio, $N(H)/A(V)$.

Our results indicate that the typical line-of-sight in the SMC is characterized by grains smaller and of a different type on the average than those in the Galaxy. This may be further evidence that the dust grains have formed and evolved somewhat differently and/or at a different rate in the SMC environment than they have in the Galaxy.

This work has been supported by NASA Grant NAG 5 1463. It has been also partially supported by FAPESP (CVR: 89/3091-6; AMM: 89/1670-9, 92/3345-0 and 94/0033-3) and CNPq (AMM: 301558/79-5). AMM and CVR would like to acknowledge the hospitality provided by Dr. A. Code, Space Astronomy Laboratory and Astronomy Department, University of Wisconsin, where this research was partly done. We would like to thank the referee, Dr. Peter Martin, for his valuable criticism which helped improve the paper.

Table 1. SMC polarization data

Identification		Observed			Corrected			
AZV	SK	P	σ_P	θ_P	P	σ_P	θ_P	λ_{eff}
(1)	(2)	(%)	(%)	($^\circ$)	(%)	(%)	($^\circ$)	(μm)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
126	-	1.149	0.095	107.5	0.737	0.126	104.1	0.379
		1.175	0.055	109.3	0.725	0.105	106.6	0.439
		1.076	0.040	111.4	0.598	0.102	109.7	0.559
		0.781	0.078	110.1	0.325	0.129	105.3	0.664
		0.825	0.083	108.6	0.407	0.120	103.7	0.791
211	74	1.207	0.044	126.6	0.943	0.085	127.3	0.378
		1.243	0.027	124.8	0.955	0.083	125.0	0.438
		1.250	0.075	126.0	0.947	0.112	126.6	0.516
		1.175	0.017	126.1	0.873	0.085	126.8	0.559
		1.063	0.018	127.6	0.774	0.082	128.9	0.664
		0.986	0.042	131.1	0.728	0.085	133.7	0.790
		0.991	0.080	125.0	0.726	0.107	125.3	0.820
215	76	0.782	0.035	148.5	0.626	0.086	158.3	0.437
		0.907	0.032	148.6	0.741	0.089	157.4	0.557
		0.742	0.033	148.5	0.587	0.087	159.2	0.662
		0.653	0.060	148.7	0.512	0.095	160.0	0.791
221	77	1.125	0.099	138.3	0.903	0.129	148.4	0.377
		1.048	0.047	140.9	0.862	0.101	153.3	0.437
		1.014	0.042	141.5	0.838	0.103	155.2	0.558
		0.799	0.060	144.3	0.698	0.109	161.6	0.663
		0.659	0.084	143.0	0.557	0.119	162.5	0.791
398	-	2.114	0.108	131.4	1.856	0.130	132.5	0.380
		2.084	0.058	132.5	1.810	0.098	133.8	0.440
		2.038	0.042	131.9	1.751	0.093	133.2	0.560
		1.948	0.058	134.6	1.679	0.099	136.4	0.665
		1.464	0.072	134.8	1.218	0.103	137.0	0.791
456	143	0.959	0.074	163.9	0.842	0.086	167.0	0.376
		1.147	0.060	160.0	1.006	0.076	162.3	0.437

Table 1—Continued

Identification		Observed			Corrected			
AZV	SK	P	σ_P	θ_P	P	σ_P	θ_P	λ_{eff}
		(%)	(%)	($^\circ$)	(%)	(%)	($^\circ$)	(μm)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
		1.323	0.172	156.7	1.156	0.179	158.4	0.516
		1.338	0.045	160.9	1.195	0.067	163.0	0.559
		1.259	0.050	160.7	1.120	0.069	162.9	0.671
		1.133	0.059	161.3	1.006	0.073	163.6	0.791
		0.950	0.089	163.2	0.830	0.099	166.2	0.820

Table 2. Foreground polarization corrections for various regions in the SMC

Region	P (%)	σ_P (%)	θ (deg)	σ_θ (deg)	N
I	0.47	0.09	113.6	14.0	6
II	0.30	0.08	124.1	8.0	10
III	0.17	0.05	145.0	8.2	11
IV	0.22	0.05	124.2	6.5	6
V	0.27	0.05	95.6	5.5	11

Table 3a. Relevant data on the reddened stars

Star	Sp	$(B - V)_0^f$	V ^g	(B-V)	(U-B)	E(B-V)	IUE Images
AZV 20	<i>A0Ia</i> ^a	-0.04	12.1	+0.29	-0.12	+0.33	LWP 21313,14,15 SWP 42509, 39,40
AZV 126	<i>B0Iw</i> ^b	-0.25	13.47	-0.02	-0.90	+0.23	LWP 21279,80 LWR 14947 SWP 42506, 18908
AZV 211	<i>A0Ia</i> ^d	-0.04	11.5	+0.10	-0.45	+0.14	LWP 21279, 80 LWR 14947 SWP 42506, 18908
AZV 398	<i>B2</i> ^e	-0.18	13.85	+0.09	-0.77	+0.27 +0.37 ^h	LWR 14963 SWP 18911
AZV 456	<i>B0 - 1</i> ^e	-0.25	12.89	+0.10	-0.74	+0.35 +0.36 ^h	LWR 12347 SWP 16051

Table 3b. Relevant data on the comparison stars

Comparison Star	Reddened Star	Sp	$(B - V)_0^f$	V ^g	(B-V)	(U-B)	IUE Images
AZV 61	AZV 126	<i>O5V</i> ^c	+0.01	13.68	-0.23	-0.98	LWP 19245
AZV 161	AZV 20 AZV 211	<i>A0Ia</i> ^a	+0.01	11.80	+0.03	-0.40	LWP 19245 SWP 40139
AZV 235	AZV 398 AZV 456	<i>B0Iw</i> ^b	-0.24	12.15	-0.12	-0.94	LWR 7239, 84 SWP 8293
AZV 242	AZV 398 AZV 456	<i>B1 : Ia</i> ^a	-0.19	12.08	-0.10	-0.88	LWR 7242 SWP 8296
AZV 270	AZV 20 AZV 211	<i>A0Ia</i> ^d	+0.02	11.43	+0.03	-0.42	LWP 19241, 44 SWP 40134, 37
AZV 289	AZV 398 AZV 456	<i>B0.5I</i> ^c	-0.22	12.42	-0.14	-0.94	LWR 12345 SWP 16049, 18829
AZV 317	AZV 126 AZV 398 AZV 456	<i>B0Iw</i> ^b	-0.24	12.90	-0.20	-1.00	LWR 17264 SWP 10315, 22373
AZV 454	AZV 126	<i>OV</i> ^e	-	-	-0.19	-0.98	LWR 14948 SWP 18909, 22016
AZV 488	AZV 398 AZV 456	<i>B0Ia</i> ^d	-0.24	11.88	-0.13	-0.97	LWR 5642 SWP 6590
AZV 504	AZV 20 AZV 211	<i>B9Ia</i> ^d	-	11.91	-0.04	-0.46	LWP 19242 SWP 40138
SK 194	AZV 20 AZV 211	<i>B9Ia</i> ^d	-	11.74	+0.02	-0.53	LWP 21282, 83 SWP 42507, 08

^aHumphreys (1983)

^bGarmany et al. (1987)

^cCrampton & Greasley (1982)

^dAndersson et al. (1979)

Table 4. Parameters of the Serkowski curve from fits of the SMC polarization data

Star	λ_{max} (μm)	$\sigma_{\lambda_{max}}$ (μm)	K	σ_K	P_{max} (%)	$\sigma_{P_{max}}$ (%)	χ^2_ν	$P(\chi^2_\nu)$	ν
AZV 126	0.31	0.31	1.0	1.8	0.79	0.34	0.73	0.48	2
	0.20	0.99	0.3	1.6	0.8	1.4	0.77	0.51	3
AZV 211	0.37	0.22	0.48	0.67	0.956	0.089	0.11	0.98	4
	0.42	0.06	0.70	0.10	0.950	0.053	0.11	0.99	5
AZV 215	0.54	0.05	2.5	1.9	0.707	0.071	0.54	0.46	1
	0.48	0.12	0.81	0.20	0.666	0.061	0.66	0.52	2
AZV 221	0.42	0.12	1.2	1.3	0.892	0.073	0.09	0.91	2
	0.34	0.14	0.57	0.23	0.910	0.140	0.13	0.94	3
AZV 398	0.46	0.04	1.26	0.55	1.87	0.07	1.15	0.32	2
	0.40	0.05	0.68	0.08	1.86	0.08	1.17	0.32	3
AZV 456	0.57	0.02	2.06	0.53	1.19	0.05	0.30	0.88	4
	0.59	0.03	0.98	0.06	1.11	0.03	1.10	0.36	5

TABLE 5
PARAMETERS OF THE SMC EXTINCTION CURVES USING EXPRESSION OF FITZPATRICK & MASSA (1990)

Star	c_1	σ_{c_1}	c_2	σ_{c_2}	c_3	σ_{c_3}	c_4	σ_{c_4}	γ (μm^{-1})	σ_γ (μm^{-1})	x_o (μm^{-1})	σ_{x_o} (μm^{-1})	A (μm^{-1})	χ^2	Bin (\AA)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)	(16)
AZV 126	-2.2	7.3	0.68	0.44	47	282	0.71	0.58	4.4	7.7	4.70	0.68	16.80	0.17	80
	-0.42	0.18	0.61	0.03	4.97	2.00	0.49	0.06	2.05	0.31	4.72	0.05	3.81	1.40	5
AZV 211	-8.6	2.8	3.09	0.52	0.17	0.95	1.1	1.6	0.5	1.3	4.24	0.27	-	0.06	80
	-8.53	0.20	3.03	0.04	0.46	0.20	1.24	0.18	0.79	0.15	4.16	0.03	-	0.75	1
	-7.70	1.70	2.96	0.37	-	-	1.10	1.60	-	-	-	-	-	0.11	80
	-7.90	0.13	2.97	0.03	-	-	1.08	0.17	-	-	-	-	-	0.80	1
AZV 398	-4.67	0.23	2.21	0.05	-0.01	0.03	1.00	0.27	0.13	0.35	4.26	0.08	-	1.03	80
	-4.63	0.02	2.18	0.01	0.01	0.01	1.05	0.02	0.095	0.09	4.60	0.01	-	5.80	1
	-4.57	0.16	2.22	0.04	-	-	1.00	0.02	-	-	-	-	-	2.54	80
	-4.73	0.02	2.23	0.01	-	-	0.95	0.02	-	-	-	-	-	7.80	1
AZV 456	-0.57	0.20	0.90	0.04	4.7	1.0	0.17	0.13	1.34	0.13	4.66	0.02	5.51	1.57	80
	-0.44	0.02	0.92	0.01	2.70	0.06	0.09	0.01	1.04	0.01	4.71	0.01	4.10	9.70	1
Seaton Curve	-0.4	2.0	0.75	0.31	4.0	4.4	0.22	0.54	1.05	0.55	4.59	0.12	5.98	0.02	-

Table 6. Parameters obtained from fits to the polarimetric data for the SMC and the Galaxy

Object/ Figure (1)	a_p^{sil} (μm) (2)	a_+^{sil} (μm) (3)	$\langle a \rangle$ (μm) (4)	Width (μm) (5)	$\delta(Si)^a$ (dex) (6)	Model (7)	Mat. (8)	γ ($^\circ$) (9)	χ^2 (10)
Gal	0.043	0.150	0.063	0.107	7.61	M79	AS	60	0.00003
Fig. 8	0.039	0.186	0.059	0.147	7.66	M79	AS	60	0.00293
	0.054	0.162	0.078	0.107	7.09	M79	AS	30	0.00035
	0.050	0.190	0.074	0.140	7.13	M79	AS	30	0.00041
	0.045	0.241	0.069	0.197	7.19	M79	AS	30	0.00267
	0.062	0.203	0.090	0.141	6.98	M79	AS	10	0.00023
	0.062	0.198	0.090	0.136	6.98	M79	AS	10	0.00027
	0.086	0.143	0.106	0.057	6.93	M79	AS	10	0.00356
	0.021	0.146	0.062	0.125	8.06	M86	AS	60	0.02490
	0.015	0.146	0.057	0.131	8.10	M86	AS	60	0.02406
	0.010	0.146	0.052	0.136	8.14	M86	AS	60	0.02394
	0.006	0.146	0.048	0.140	8.17	M86	AS	60	0.02395
	0.042	0.129	0.075	0.087	7.37	M86	AS	30	0.01162
	0.026	0.146	0.066	0.120	7.44	M86	AS	30	0.01045
	0.020	0.148	0.061	0.128	7.48	M86	AS	30	0.01037
	0.010	0.148	0.052	0.138	7.54	M86	AS	30	0.01031
	0.083	0.139	0.106	0.056	7.01	M86	AS	10	0.00312
	0.061	0.163	0.095	0.101	7.08	M86	AS	10	0.00058
	0.030	0.179	0.073	0.149	7.22	M86	AS	10	0.00076
AZV398	0.031	0.149	0.048	0.119	6.46	M79	AS	60	1.62
Fig. 10	0.037	0.172	0.057	0.135	5.96	M79	AS	30	1.57
	0.060	0.136	0.081	0.076	5.75	M79	AS	10	1.11
	0.043	0.088	0.056	0.046	6.56	M79	ENS	60	0.34
	0.045	0.186	0.069	0.141	6.21	M79	ENS	30	1.50
	0.061	0.099	0.075	0.038	6.07	M79	ENS	30	0.34
	0.076	0.141	0.098	0.065	5.99	M79	ENS	10	1.26
	0.031	0.082	0.047	0.051	6.64	M86	AS	60	0.48
	0.009	0.140	0.032	0.131	6.79	M86	AS	60	2.36
	0.031	0.168	0.053	0.137	6.10	M86	AS	30	1.63
	0.034	0.202	0.058	0.168	5.94	M86	AS	10	1.69
	0.031	0.162	0.054	0.131	6.89	M86	ENS	60	1.71
	0.042	0.089	0.057	0.047	6.77	M86	ENS	60	0.59
	0.042	0.195	0.066	0.153	6.31	M86	ENS	30	1.58

Table 6—Continued

Object/ Figure (1)	a_p^{sil} (μm) (2)	a_+^{sil} (μm) (3)	$\langle a \rangle$ (μm) (4)	Width (μm) (5)	$\delta(Si)^a$ (dex) (6)	Model (7)	Mat. (8)	γ ($^\circ$) (9)	χ^2 (10)
	0.062	0.098	0.075	0.036	6.14	M86	ENS	30	0.38
	0.078	0.136	0.098	0.058	5.99	M86	ENS	10	1.44
AZV456	0.045	0.145	0.066	0.108	7.10	M79	AS	60	6.43
Fig. 12	0.056	0.160	0.080	0.104	6.58	M79	AS	30	7.24
	0.099	0.131	0.112	0.032	6.40	M79	AS	10	1.93
	0.109	0.166	0.131	0.057	7.56	M79	ENS	60	2.21
	0.047	0.202	0.072	0.155	7.41	M79	ENS	60	10.07
	0.131	0.173	0.149	0.042	6.99	M79	ENS	30	12.94
	0.062	0.192	0.090	0.130	6.87	M79	ENS	30	10.29
	0.084	0.200	0.116	0.116	6.71	M79	ENS	10	4.67
	0.112	0.145	0.126	0.032	6.65	M79	ENS	10	1.72
	0.038	0.144	0.075	0.107	7.51	M86	AS	60	11.44
	0.047	0.157	0.084	0.111	6.87	M86	AS	30	10.72
	0.055	0.184	0.094	0.129	6.65	M86	AS	10	6.52

^aThe observed values of the Si/H abundance for the Galaxy (Anders & Grevesse 1989) and the SMC (Dufton et al. 1990) are 7.55 and 6.88, respectively.

Note. — Columns: (1) The object name in the Azzopardi & Vigneau (1982) catalogue; (2) The minimum size of cylindrical grain; (3) The maximum size of cylindrical grain; (4) Average size; (5) Width of the size distribution which corresponds to the difference between the two size parameters; (6) Silicon abundance needed to reproduce the degree of polarization; (7) Models: M79 (Mathis 1979) or M86 (Mathis 1986); (8) Material used in the calculations: AS (astronomical silicate) or ENS (Enstatite). See Sec. 2 for references; (9) Angle between the magnetic field and the plane of sky and (10) The value of χ^2 is not divided by N.

Note. — The fits in bold-face type are plotted in the figures whose numbers are given in column 1.

TABLE 7
PARAMETERS OBTAINED FITTING EXTINCTION CURVES

Obj	Model	γ ($^{\circ}$)	Cont	C Depl.	Silicate			Carbon		χ^2	Esf.	Si fraction		$\frac{P(V)}{A(V)}$	
					a_{-}^{sil} (μm)	a_p^{sil} (μm)	a_{+}^{sil} (μm)	a_{-}^{car} (μm)	a_{+}^{car} (μm)			Cyl.	Total	Model ($\frac{\%}{mag}$)	Obs. ($\frac{\%}{mag}$)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)	(16)
Gal Fig. 9	M79/AS+GR	60	v	0.7	0.0174	0.043	0.150	0.0002	0.292	0.8	0.27	0.64	0.90	1.72	1.61
	M79/AS+GR	60	v	0.7	0.0124	0.039	0.186	0.0001	0.262	1.2	0.26	0.72	0.97	1.62	1.61
	M79/AS+GR	10	v	0.7	0.0151	0.086	0.143	0.0027	0.187	2.4	0.48	0.24	0.72	3.49	2.90
	M86/AS+GR	60	v	0.7	0.0046	0.021	0.146	0.0003	0.300	1.7	0.24	0.72	0.96	0.72	0.64
	M86/AS+GR	30	v	0.7	0.0205	0.042	0.129	0.0001	0.301	0.9	0.27	0.66	0.93	3.17	2.90
	M86/AS+GR	30	v	0.7	0.0080	0.026	0.146	0.0001	0.306	2.4	0.25	0.78	1.03	3.12	2.90
	M86/AS+GR	10	v	0.8	0.0241	0.083	0.139	0.0068	0.259	1.3	0.45	0.29	0.74	3.09	2.90
	M86/AS+GR	10	v	0.8	0.0096	0.061	0.163	0.0035	0.170	3.1	0.33	0.34	0.67	3.04	2.90
AZV398 Fig. 11	M79/AS+AC	60	v	1.0	0.0234	0.031	0.149	0.0148	0.021	57.0	0.04	0.38	0.42	2.05	2.01
	M79/AS+AC	30	s	1.0	0.0001	0.037	0.172	0.0123	0.041	157	0.03	0.12	0.15	2.56	2.01
	M79/AS+AC	10	v	1.0	0.0119	0.060	0.136	0.0079	0.048	172.	0.08	0.07	0.15	2.60	2.01
	M79/EN+GR	60	v	0.4	0.0035	0.043	0.088	0.0372	0.140	29.4	0.79	0.48	1.27	1.89	2.01
	M79/EN+AC	60	v	0.8	0.0101	0.043	0.088	0.0036	0.531	50.8	0.57	0.48	1.05	1.84	2.01
	M79/EN+AC	30	v	1.0	0.0001	0.045	0.186	0.0040	0.050	113	0.20	0.21	0.41	2.48	2.01
	M79/EN+AC	30	v	0.8	0.0001	0.061	0.099	0.0025	0.111	27.0	0.54	0.15	0.69	1.98	2.01
	M79/EN+AC	10	v	1.0	0.0001	0.076	0.141	0.0003	0.062	105.	0.34	0.13	0.47	2.64	2.01
	M86/AS+AC	60	v	0.5	0.0001	0.009	0.140	0.0125	0.014	50.7	0.25	0.81	1.06	2.15	2.01
	M86/AS+AC	10	v	1.0	0.0056	0.034	0.202	0.0112	0.043	163.	0.05	0.11	0.16	2.54	2.01
AZV456 Fig. 13	M79/EN+GR	60	s	0.15	0.0180	0.109	0.166	0.011	0.041	66.5 ^a	0.68	0.80	1.48	1.35	1.34

^aAssuming $N(H)/A(V)=4.1 \cdot 10^{22} \text{ cm}^{-2}$. See sec. 5.3.2.

NOTE.— Columns: (1) Object; (2) Model for the polarizing grains (M79 or M86) and composition of the grains (AS stands for Astronomical Silicate, EN for ENstatite, GR for GRaphite and AC for Amorphous Carbon); (3) Angle between the the magnetic field and the plane of sky; (4) The continuity adopted: "s", size continuity and "v", volume continuity (see sec. 5); (5) Carbon depletion as a fraction of the available ISM abundance; (6) Minimum size of spherical silicate grains; (7) Maximum size of spherical silicate grains (= Minimum size of cylindrical silicate grains); (8) Maximum size of cylindrical silicate grains; (9) Minimum size of carbon grains; (10) Maximum size of carbon grains; (11) Reduced χ^2 as a parameter of the fit quality; Si fraction abundances relative to the available in the SMC in form of spherical grains (12), cylindrical grains (13) and total fraction (14); (15) $P(V)/A(V)$ obtained from the fit; (16) Observed $P(V)/A(V)$.

NOTE.—The entries in bold-face type are plotted in the figures whose numbers are given in column 1.

REFERENCES

- Anders, E. & Grevesse, N. 1989, *Geochimica et Cosmochimica Acta* 53, 197
- Anderson, C.M. et al. 1996, *ApJ*, submitted.
- Andersson, B.-G. & Wannier, P.G. 1995, *ApJ*443, L49
- Azzopardi, M. & Vigneax, J. 1982, *A&AS*50, 291 (AZV82)
- Bessel, M.S. 1991, *A&A*242, L17
- Blanco, A., Fonti, S. & Orofino, V. 1995, *ApJ*448, 339
- Boggess, A. et al. 1978a, *Nature* 275, 372
- Boggess, A. et al. 1978b, *Nature* 275, 377
- Bohlin, R.C. & Grillmair, C.J. 1988a, *ApJS*66, 209
- Bohlin, R.C. & Grillmair, C.J. 1988b, *ApJS*68, 487
- Bohlin, R.C. Savage, B.D. & Drake, J.F. 1978, *ApJ*224, 132
- Bouchet, P., Lequeux, J., Maurice, E., Prévot, L. & Prévot-Burnichon, M.L. 1985, *A&A*149,330
- Bromage, G. E. & Nandy, K. 1983, *MNRAS*204, 29p
- Brunet, J. P. 1975, *A&A*43, 345
- Burton, W.B., Deul, E.R., Walker, H.J. & Jongeneelen, A.A.W. 1986, in *Light on Dark Matter*, ed. F.P. Israel (Dordrecht: Reidel), 357
- Buss Jr., R. H., Lamers, H. J. G. L. M. & Snow Jr., T. P. 1989, *ApJ*347, 977
- Bussoletti, E., Colangeli, L. & Orofino 1988, in *Experiments Cosmic Dust Analogues*, ed. E. Bussoletti, C. Fusco & G. Longo (Netherlands: Kluwer Ac. Publ.), 63
- Cardelli, J.A. & Clayton, G.C. 1991, *AJ*101, 1021
- Cardelli, J.A., Clayton, G.C. & Mathis, J.S. 1989, *ApJ*345, 245
- Cardelli, J.A. & Savage, B.D. 1988, *ApJ*325, 864
- Casey, S. 1991, *ApJ*371, 183
- Chini, R. & Krügel, E. 1983, *A&A*117, 289
- Chlewicki, G. & Greenberg, J. M. 1990, *ApJ*365, 230

- Clarke, D. & Stewart, B.G. 1986, *Vistas in Astronomy* 29, 27
- Clayton, G.C., Anderson, C.M., Magalhães, A.M., Code, A.D., Nordsiek, K.H., Meade, M.R., Wolff, M.J., Babler, B., Biorkman, K.S., Schulte-Ladbeck, R.E., Taylor, M. & Whitney, B.A. 1992, *ApJ*385, L53
- Clayton, G.C., Green, J., Wolff, M., Zellner, N., Code, A.D. & Davidsen, A. 1996, *ApJ*, in press.
- Clayton, G.C. & Martin, P.G. 1985, *ApJ*288, 558
- Clayton, G.C., Martin, P.G. & Thomson, I. 1983, *ApJ*265, 194
- Clayton, G.C. & Mathis, J.S. 1988, *ApJ*327, 911
- Clayton, G.C., Wolff, M., Allen, R.G. & Lupie, O.L. 1995, *ApJ*445, 947
- Codina-Landaberry, S. & Magalhães, A.M. 1976, *A&A*49, 407
- Coyne, G.V., Gehrels, T. & Serkowski, K. 1974, *AJ*79, 581
- Désert, F.-X., Boulanger, F. & Puget, J.L. 1990, *A&A*237, 215
- Draine, B. T. & Lee, H. M. 1984, *ApJ*285, 89
- Draine, B. T. & Malhotra, S. 1993, *ApJ*414, 632
- Dufton, P. L., Fitzsimmons, A. & Howarth, I. D. 1990, *ApJ*362, L59
- Duley, W. W. 1984, *ApJ*287, 694
- Fitzgerald, M.P. 1970, *A&A*4, 234
- Fitzpatrick, E.L. 1985a, *ApJ*299, 219
- Fitzpatrick, E.L. 1985b, *ApJS*59, 77
- Fitzpatrick, E.L. 1986, *AJ*92, 1068
- Fitzpatrick, E.L. 1989, in *IAU Symposium 135, Interstellar Dust*, ed. L.J. Allamandola & A.G.G.M. Tielens (Dordrecht: Kluwer), 37
- Fitzpatrick, E.L. & Massa, D., 1986, *ApJ*307, 286
- Fitzpatrick, E.L. & Massa, D., 1988, *ApJ*328, 734
- Fitzpatrick, E.L. & Massa, D. 1990, *ApJS*72, 163
- Frecker, J. & Serkowski, K. 1976, *Appl.Opt.* 15, 605

- Gehrz, R.D. 1989, in IAU Symp. 135: "Interstellar Dust," ed. L.J. Allamandola & A.G.G.M. Tielens (Kluwer), p. 445.
- Greenberg, J.M. & Chlewicki, G. 1983, ApJ272, 563
- Hecht, J., Holm, A. V., Donn, B. & Wu, C. C. 1984, ApJ280, 228
- Huffman, D. R. & Stapp, J. L. 1971, Nature Phys. Sci. 229, 45
- Jenniskens, P., Baratta, G.A., Kouchi, A., de Groot, M.S., Greenberg, J.M. & Strazzulla, G. 1993, A&A273, 583
- Jenniskens, P., Ehrefreund, P. & Désert, F.-X. 1992, A&A265, L1
- Jenniskens, P. & Greenberg, J.M. 1993, A&A274, 439
- Jones, R. V. & Spitzer Jr., L. 1967, ApJ147, 943
- Kim, S.-H. & Martin, P. G. 1994, ApJ431, 783
- Kim, S.-H. & Martin, P. G. 1995, ApJ444, 293
- Kim, S.-H. & Martin, P. G. 1996, ApJ462, 296
- Kim, S.-H., Martin, P. G & Hendry, P. D. 1994, ApJ422, 164
- Koorneef, J. 1982, A&A107, 247.
- Koorneef, J. & Code, A.D. 1981, ApJ247, 860
- Kondo, Y. 1987, Exploring the Universe with the IUE Satellite (Netherlands: Kluwer)
- Leene, A. & Cox, P. 1987, A&A174, L1
- Lequeux, J. 1988, in Dust in the Universe, ed. E. M. Bailey & D. A. Williams (Cambridge: Cambridge Univ. Press), 449
- Lequeux, J. 1989, in Recent Developments of Magellanic Cloud Research, ed. K.S. de Boer, F. Spite & G. Stasinska, (Paris: Obs. Paris), 119
- Lequeux, J. 1994, A&A287, 368
- Lequeux, J., Le Bourlot, J., Des Forets, G. P., Roueff, E., Boulanger & Rubio, M. 1994, A&A292, 371
- Lequeux, J., Maurice, E., Prévot, L., Prévot-Burnichon, M. L. & Rocca-Volmerange B. 1984, A&A113, L5
- Maccioni, A. & Perinotto, M. 1994, A&A284, 241

- Magalhães, A.M., Benedetti, E. & Roland, E.H. 1984, PASP96, 383
- Magalhães, A.M., Loiseau, N., Rodrigues, C.V. & Piirola, V. 1990, in IAU Symposium 140, Galactic and Intergalactic Magnetic Fields, ed. R. Beck, P.P. Kronberg & R. Wielebinski (Dordrecht: Kluwer), 255
- Magalhães, A.M., Rodrigues, C.V., Margoniner, V.E., Pereyra, A. & Heathcote, S. 1996, in Polarimetry of the Interstellar Medium, ed. D.C.B. Whittet & W. Roberge (San Francisco: ASP), in press.
- Martin, N., Maurice, E. & Lequeux, J. 1989, A&A215, 219
- Mathewson, D.S. & Ford, V.L. 1970 AJ75, 778
- Mathis, J. 1979, ApJ232, 747
- Mathis, J. 1986, ApJ308, 281 (M86)
- Mathis, J.S. 1994, ApJ422, 176
- Mathis, J.S., Ruml, W. & Nordsieck, K.H. 1977, ApJ217, 425 (MRN)
- McNamara, D.H. & Feltz, K.H. 1980, PASP92, 587
- Mennella, V., Colangeli, L., Bussoletti, E., Monaco, G., Palumbo, P. & Rotundi, A. 1995, ApJS100, 149
- Nandy, K., Morgan, D.H., Willis, A.J., Wilson, R., Gondhalekar, P.M. 1981, MNRAS196, 955
- Nuth, J. A. 1985, Nature 318, 166
- Pagel, B.E.J. 1993, in News Aspects of Magellanic Cloud Research, eds. B. Baschek, G. Klare and J. Lequeux (Berlin: Springer-Verlag), 330
- Pei, Y. C. 1992, ApJ395, 130
- Prévot, M. L., Lequeux, J., Maurice, E., Prévot, L. & Rocca-Volmerange, B. 1984, A&A132, 389
- Rice, W., Lonsdale, C.J., Soifer, B.T., Neugebauer, G., Kaplan, E.L., Lloyd, L.A., de Jong, T. & Habing, H.J. 1988, ApJS68, 91
- Rodrigues, C.V. 1992, MSc Thesis, Instituto Astronômico e Geofísico, Universidade de São Paulo
- Sanduleak, N. 1968 AJ73, 246
- Sanduleak, N. 1969 AJ74, 877
- Sauvage, M., Thuan, T.X. & Vigroux, L. 1990, A&A237, 296

- Savage, B. D. & Mathis, J. 1979, ARA&A17, 73
- Schmidt, Th. 1976, A&AS24, 357
- Schwering, P.B.W. 1988, Ph.D. Thesis, University of Leiden
- Schwering, P.B.W. & Israel, F.P. 1989, A&AS79, 79
- Seaton, M.J. 1979, MNRAS 187, 73p
- Serkowski, K. 1973, IAU Symp. 52, Interstellar Dust and Related Topics, ed. J. M. Greenberg & H.C. van de Hulst (Dordrecht: Reidel), 145
- Serkowski, K., Mathewson, D.S., & Ford, V.L. 1975, ApJ196, 261
- Sorrell, W. H. 1990, MNRAS243, 570
- Stahl, O., Buzzoni, B., Kraus, G., Schwarz, H., Metz, K., & Roth, M. 1986, The Messenger 46, 23
- Wheeler, J. C., Sneden, C. & Truran Jr., J. W. 1989, ARA&A27, 279
- Westerlund, B. E. 1989, in Recent Developments of Magellanic Cloud Research, ed. K.S. de Boer, F. Spite & G. Stasinska, (Obs. Paris: Paris), 159.
- Westerlund, B. E. 1990, Astron. Astrophys. Rev. 2, 29
- Whittet, D.C.B. & van Breda, I.G. 1978, A&A66, 57
- Whittet, D.C.B., Martin, P., Hough, J. Rouse, M. Bailey, J. & Axon, D. 1992, ApJ386, 562
- Wilking, B.A., Lebofsky, M.J., Martin, P.G., Rieke, G.H. & Kemp, J.C. 1980, ApJ235, 905
- Wilking, B.A., Lebofsky, M.J. & Rieke, G. H. 1982, AJ87, 905
- Wolff, M.J., Clayton, G.C., Martin, P.G. & Schulte-Ladbeck, R.E. 1994, ApJ423, 412
- Xu, C. & Helou, G. 1994, ApJ426, 109

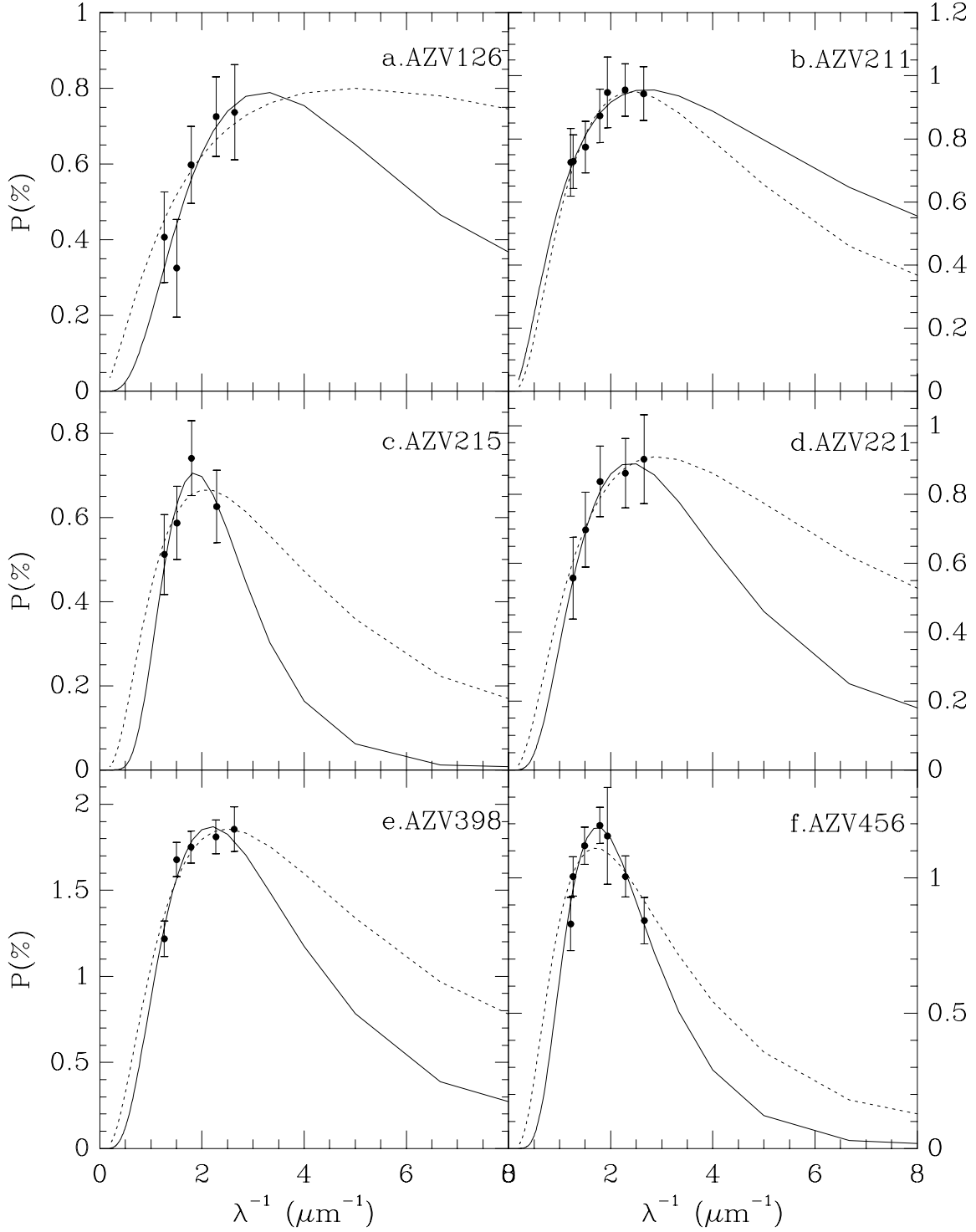


Fig. 1.— Polarization for the SMC stars. Points with error bars represent our foreground corrected data. The solid lines and dashed lines show the 3- and 2-parameter Serkowski fits, respectively.

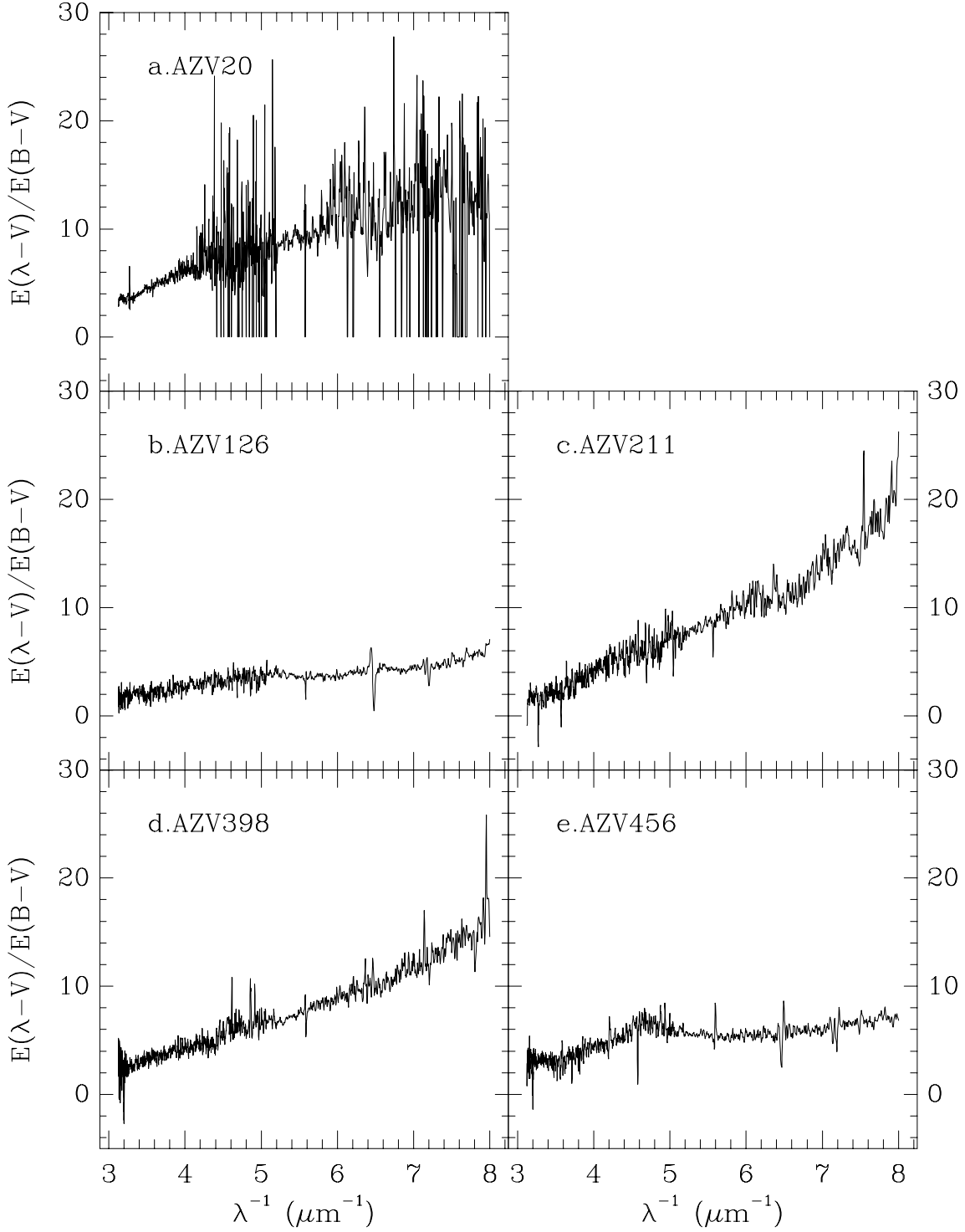


Fig. 2.— Extinction curves of SMC stars obtained using the pair-method and combined spectra with 1 Å sampling (except for 5 Å sampling for AZV 126). The curves for AZV 398 and AZV 456 were derived using in part IUE images of these objects obtained by Prévot et al. (1984) and Lequeux et al. (1984).

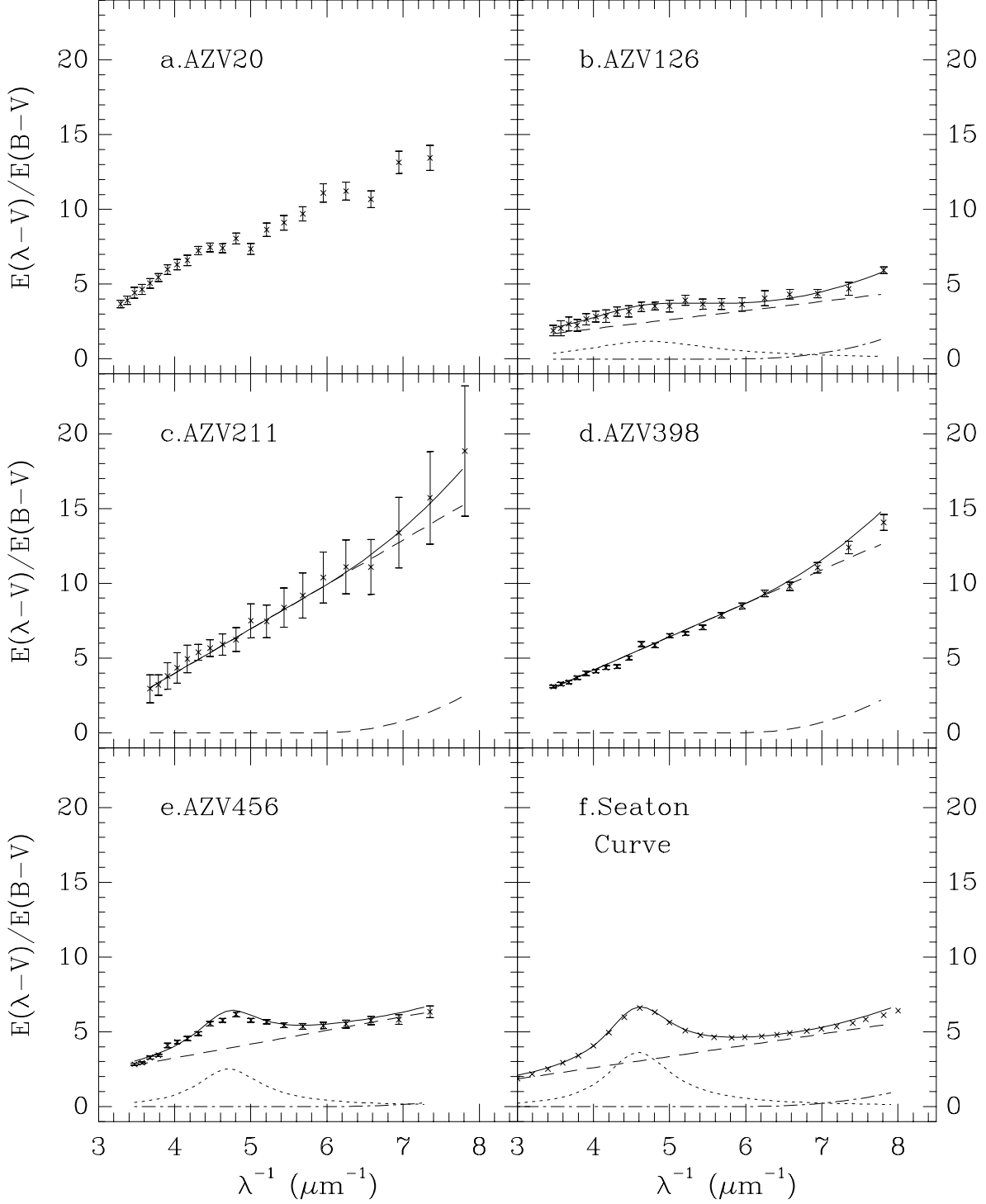


Fig. 3.— Parametric fits, using the Fitzpatrick & Massa (1986) representation, to the extinction curves for: AZV 20, 126, 211, 398, 456 and the Seaton curve for the Galaxy. The fits (solid line) were made to the extinction curve with a sampling of 1 \AA (except for 5 \AA sampling for AZV 126). The points with error bars represent the extinction curve with a binning of 80 \AA . The respective

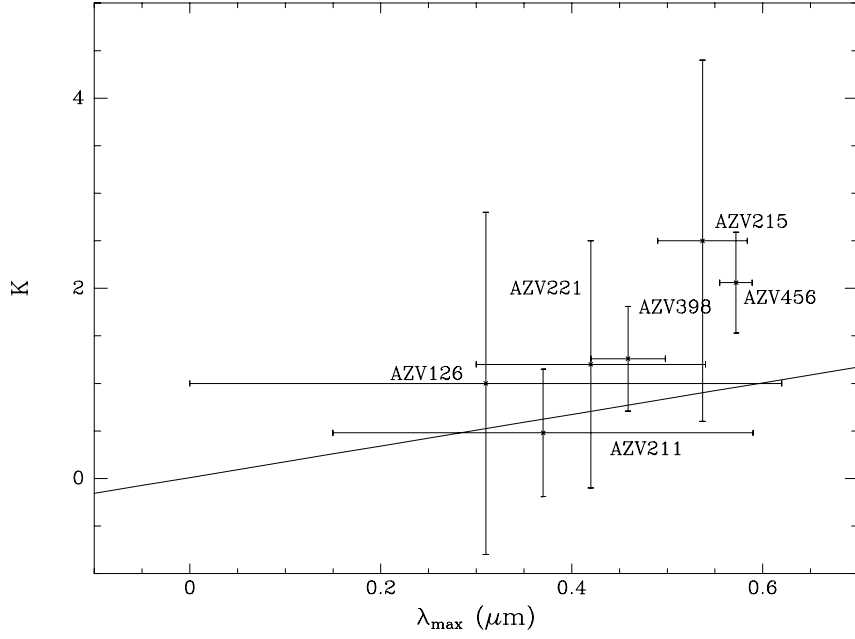


Fig. 4.— K versus λ_{\max} for SMC stars (this work) from the 3-parameter fits. The solid line is the Galactic relationship (Whittet et al. 1992).

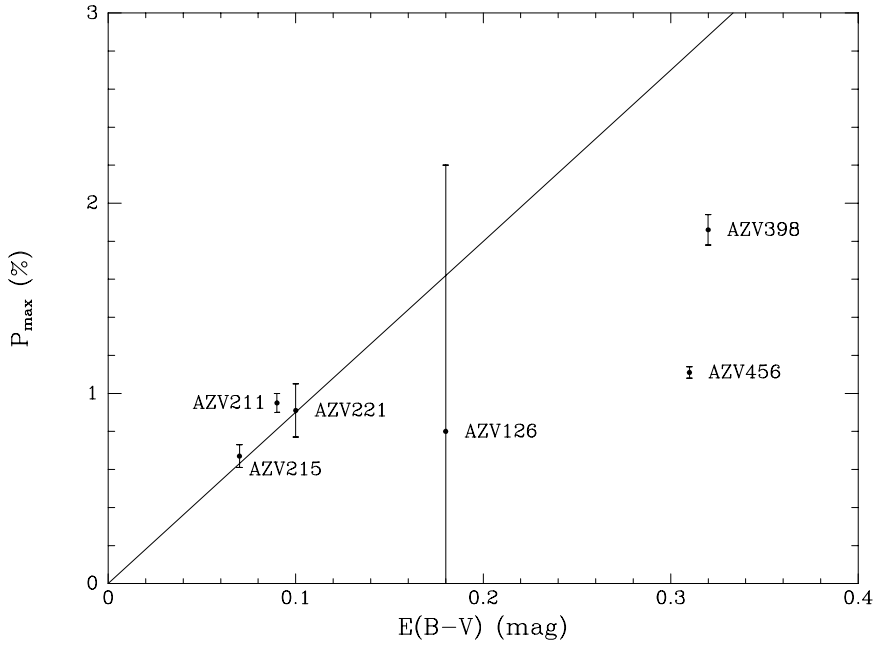


Fig. 5.— Polarization vs. $E(B - V)$. The continuous line represents the Galactic upper limit. See text (sec. 3.2) for discussion.

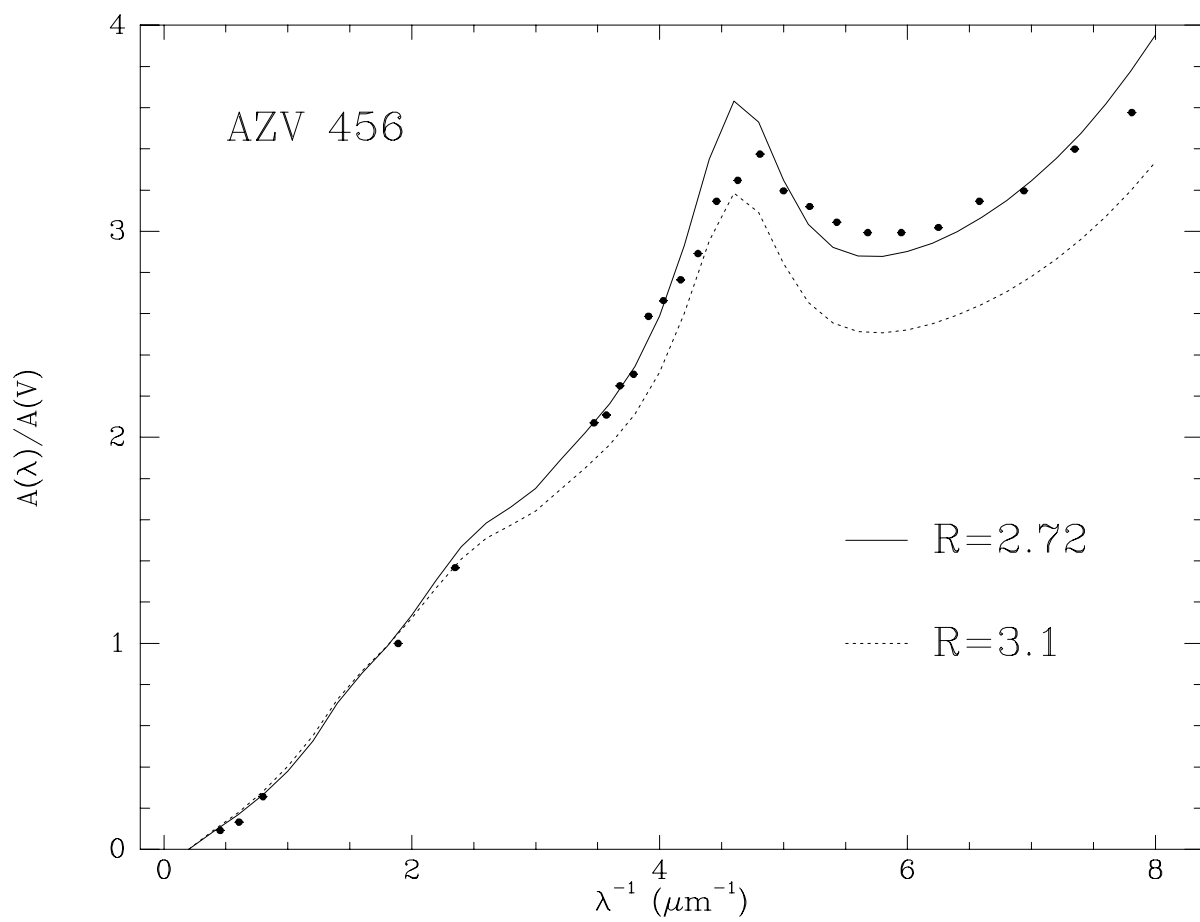


Fig. 6.— The extinction curve of AZV 456 with the analytical curves of Cardelli et al. (1989) for $R=2.72$ (solid line) and $R=3.1$ (dashed line) superimposed.

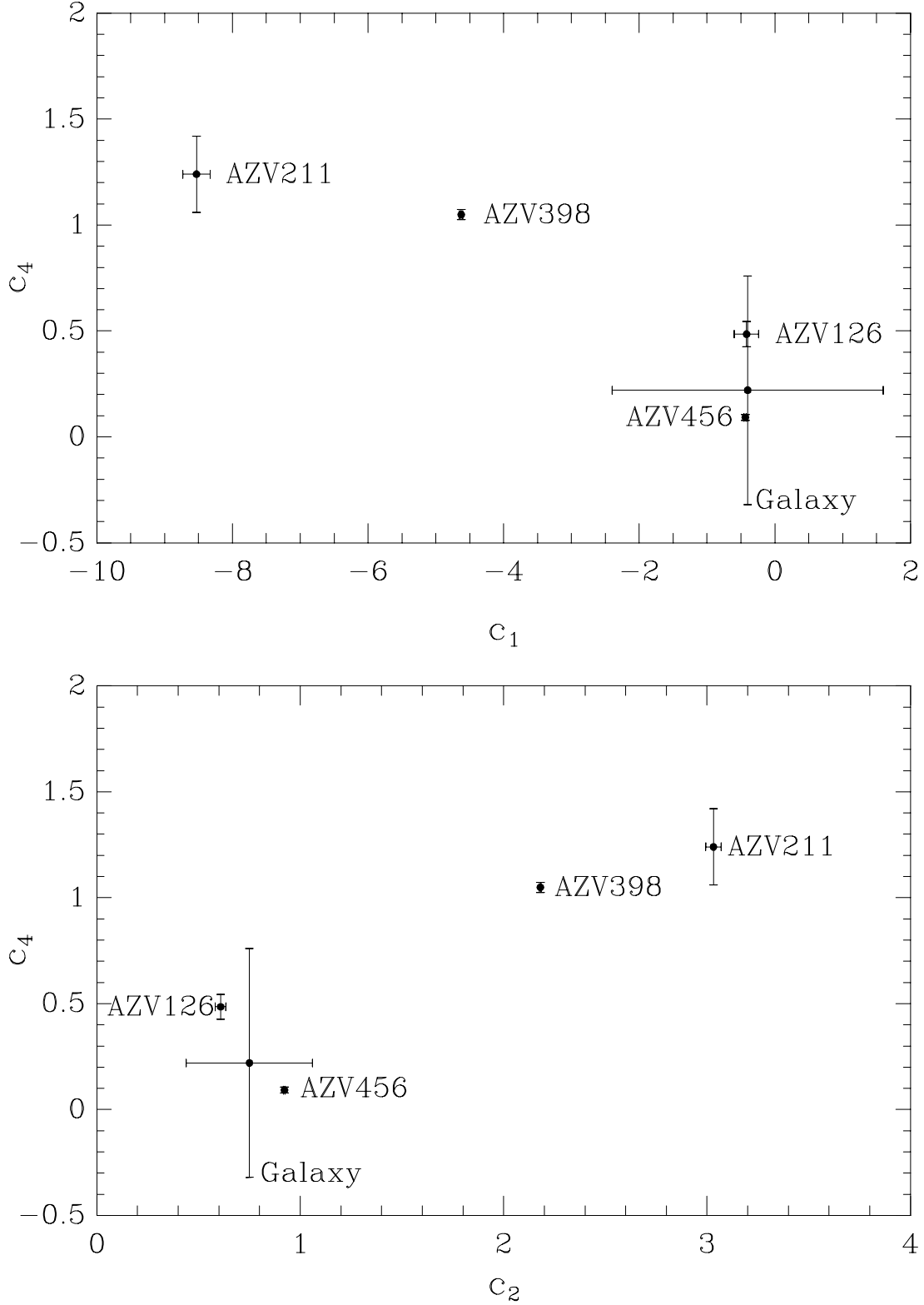


Fig. 7.— The coefficient, c_4 , for the exponential UV and FUV parts of the extinction curve plotted against the coefficients, c_1 and c_2 , respectively, for the linear part of the extinction curve. See eq. 5.

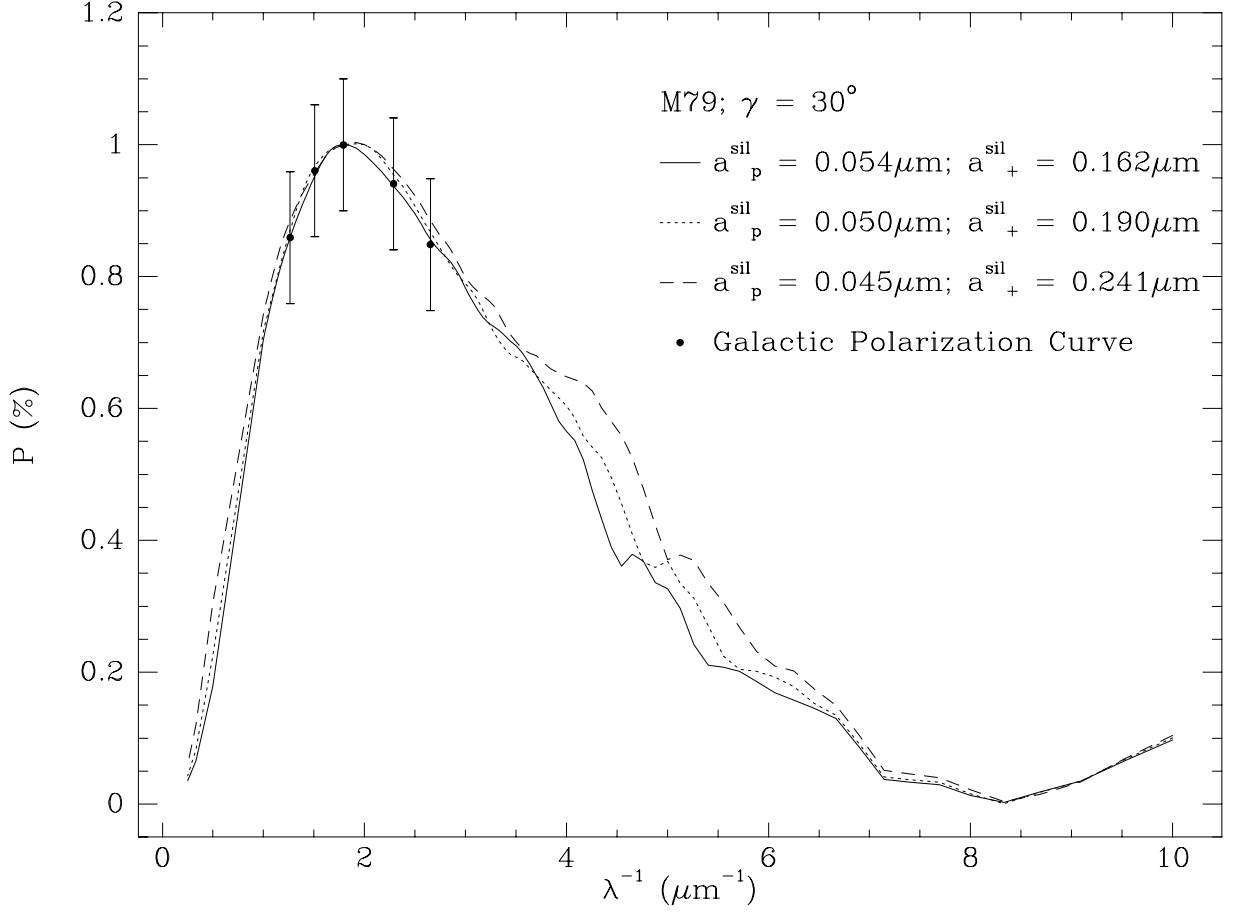


Fig. 8.— Fits to the Galactic polarization curve for $\gamma = 30^\circ$. The different curves are for size parameters representing local χ^2 minima (Table 6).

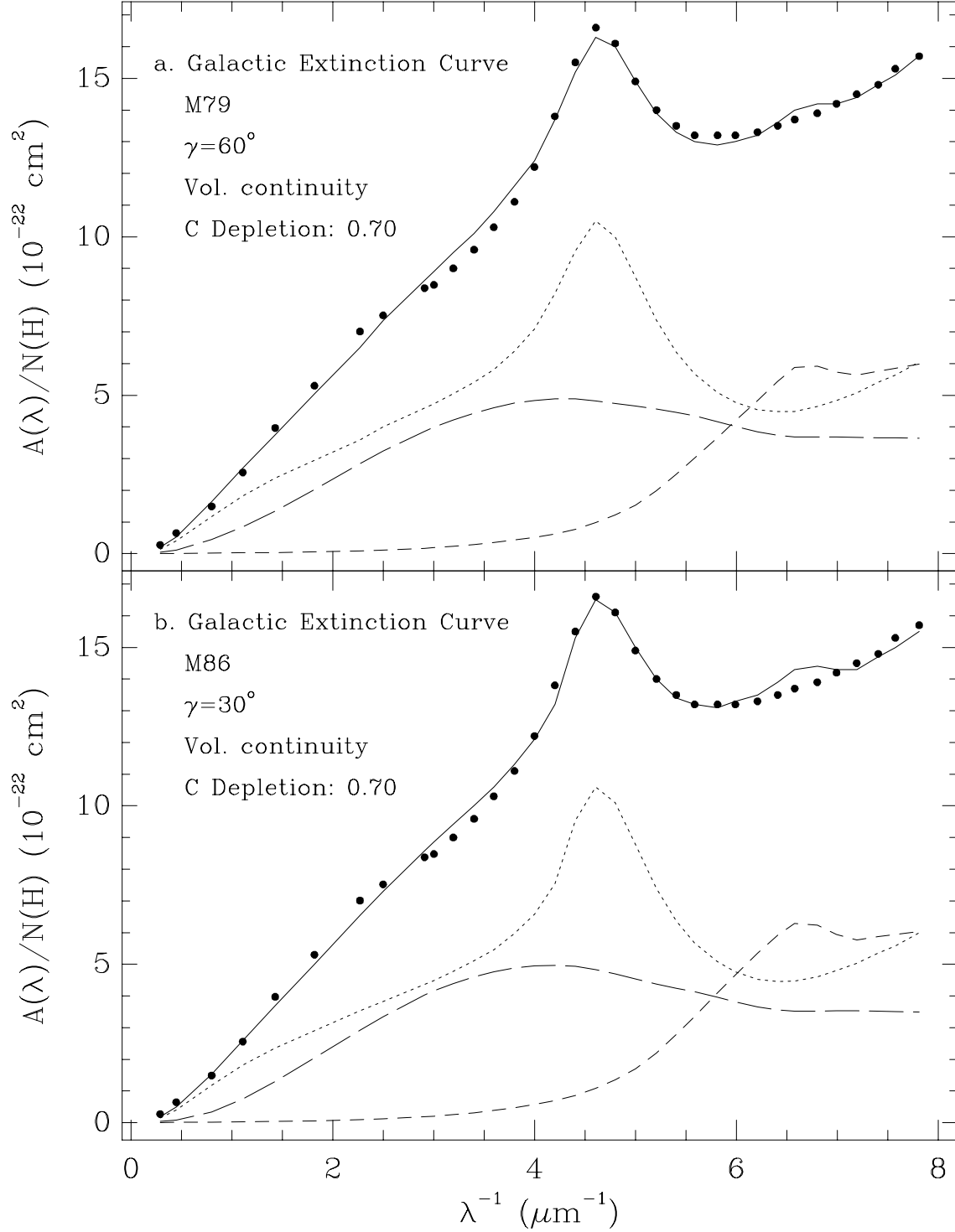


Fig. 9.— Best fits to the Galactic extinction curve (solid dots) using cylinder sizes derived from the M79 (a) or M86 (b) model fits. Additional fit parameters are given in Table 7. The dotted line represents the contribution of graphite; the long dashed line, the contribution of silicate cylinders; the short dashed line, the contribution of silicate spheres and the solid line the total extinction.

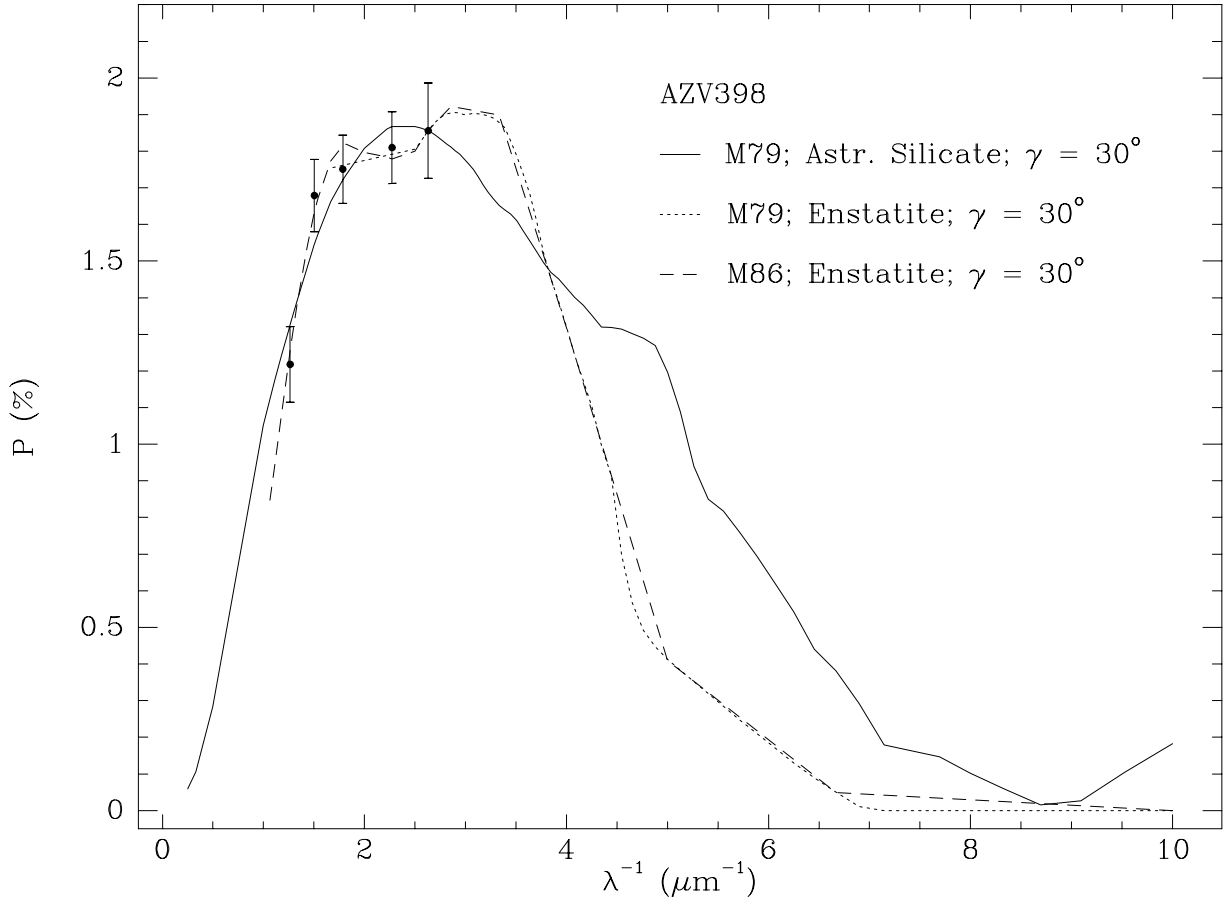


Fig. 10.— Fits to the AZV 398 polarization curve. Fit parameters are given in Table 6.

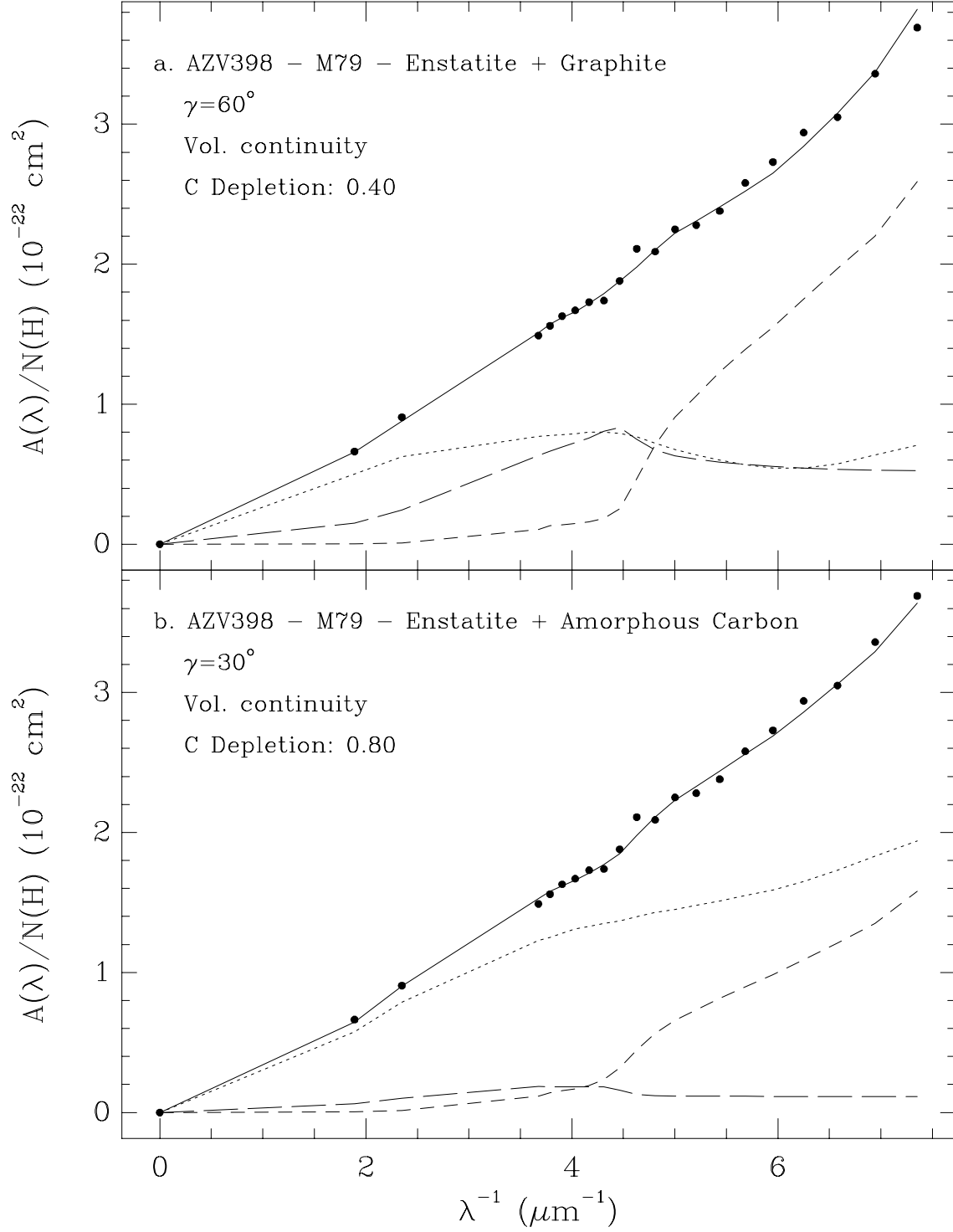


Fig. 11.— Best fits to the AZV 398 extinction curve using graphite (a) or amorphous carbon (b). Fit parameters are given in Table 7. Line styles are as in Fig. 9.

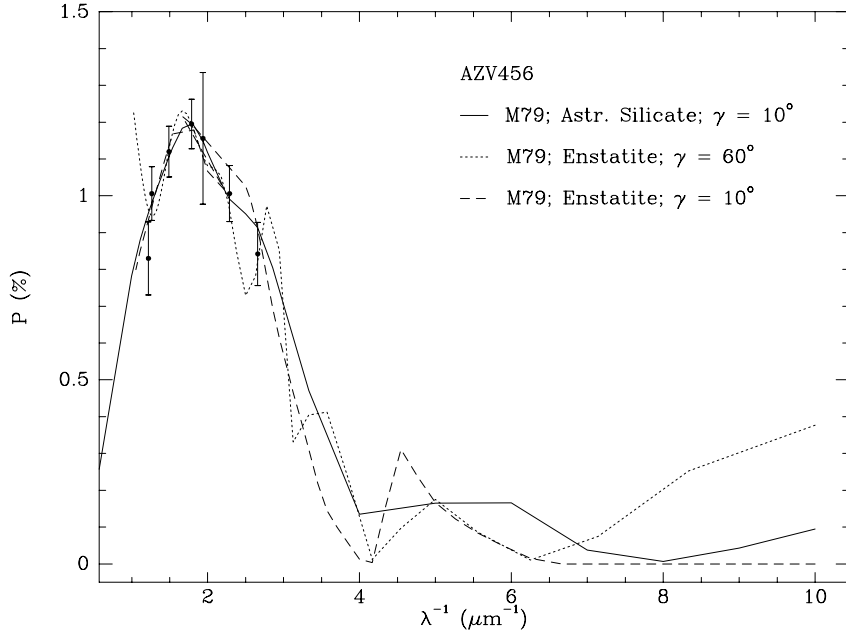


Fig. 12.— Fits to the AZV 456 polarization curve. Fit parameters are given in Table 6.

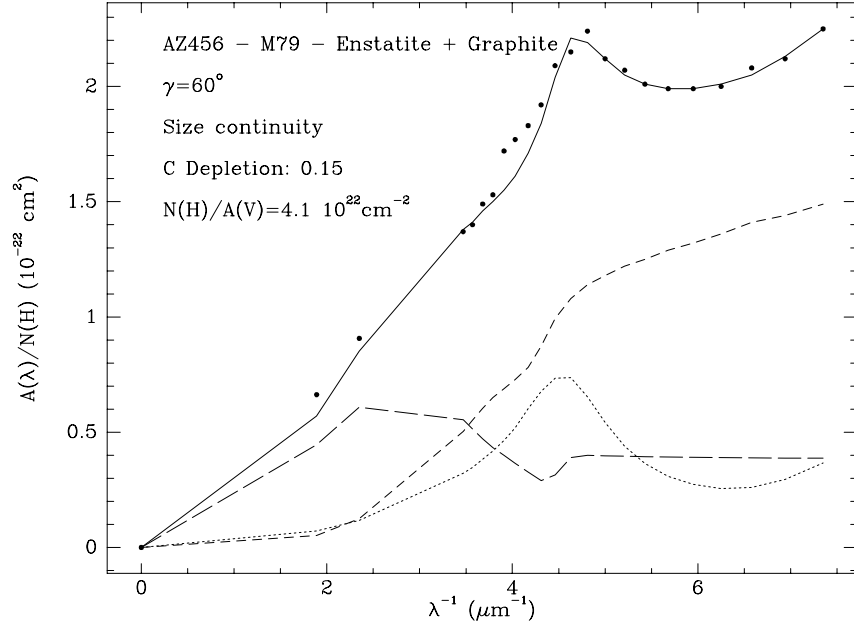


Fig. 13.— The AZV 456 extinction curve, assuming that the gas-to-dust ratio equals the $N(\text{HI})/A(V)$ ratio typical of the SMC, that of AZV398. Dust parameters for the calculated solid line are given in Table 7. Line styles are: dotted = graphite; long-dashed = silicate cylinders and short-dashed = silicate spheres.